

(12) INTERNATIONAL APPLICATION PUBLISHED UNDER THE PATENT COOPERATION TREATY (PCT)

(19) World Intellectual Property Organization  
International Bureau



(43) International Publication Date  
20 December 2001 (20.12.2001)

PCT

(10) International Publication Number  
WO 01/97008 A1

(51) International Patent Classification<sup>7</sup>: G06F 7/60

(21) International Application Number: PCT/US00/16270

(22) International Filing Date: 14 June 2000 (14.06.2000)

(25) Filing Language: English

(26) Publication Language: English

(63) Related by continuation (CON) or continuation-in-part (CIP) to earlier application:

US 09/333,625 (CON)  
Filed on 15 June 1999 (15.06.1999)

(72) Inventors; and

(75) Inventors/Applicants (for US only): RATTEREE, Michael, S. [US/US]; 14465 Willow Bend Park, Chesterfield, MO 63017-8257 (US). DUFFY, John, B. [US/US]; 14927 Lake Manor Court, Chesterfield, MO 63017 (US).

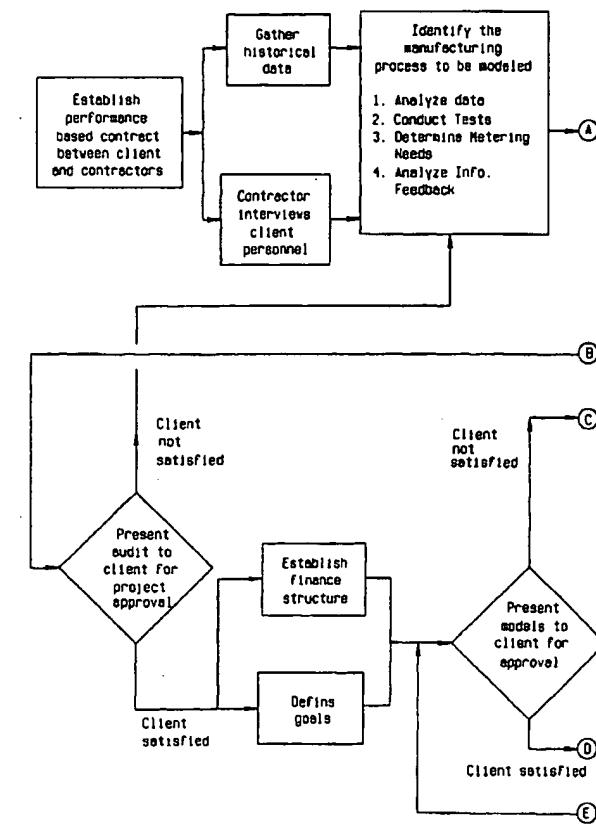
(74) Agents: DUNLAP, Charles, E. et al.; Suite 1400, 7733 Forsyth Boulevard, St. Louis, MO 63105-1817 (US).

(81) Designated States (national): AE, AG, AL, AM, AT, AU, AZ, BA, BB, BG, BR, BY, CA, CH, CN, CR, CU, CZ, DE, DK, DM, DZ, EE, ES, FI, GB, GD, GE, GH, GM, HR, HU, ID, IL, IN, IS, JP, KE, KG, KP, KR, KZ, LC, LK, LR, LS, LT, LU, LV, MA, MD, MG, MK, MN, MW, MX, NO, NZ, PL, PT, RO, RU, SD, SE, SG, SI, SK, SL, TJ, TM, TR, TT, TZ, UA, UG, US, UZ, VN, YU, ZA, ZW.

(84) Designated States (regional): ARIPO patent (GH, GM, KE, LS, MW, SD, SL, SZ, TZ, UG, ZW), Eurasian patent (AM, AZ, BY, KG, KZ, MD, RU, TJ, TM), European patent

[Continued on next page]

(54) Title: PERFORMANCE-BASED METHOD FOR OBTAINING SAVINGS IN AN INDUSTRIAL PROCESS



(57) Abstract: A method for obtaining savings in an industrial process (Fig. 1) includes the steps of establishing a performance-based contract between the owner of the industrial process and a contractor (Fig. 1); deriving with a computer a statistical mathematical model that describes a productivity-related parameter for the industrial process (Fig. 1); identifying a modification that will improve the productivity-related parameter (Fig. 1); and implementing the modification (Fig. 1).

WO 01/97008 A1



(AT, BE, CH, CY, DE, DK, ES, FI, FR, GB, GR, IE, IT, LU, MC, NL, PT, SE), OAPI patent (BF, BJ, CF, CG, CI, CM, GA, GN, GW, ML, MR, NE, SN, TD, TG).

*For two-letter codes and other abbreviations, refer to the "Guidance Notes on Codes and Abbreviations" appearing at the beginning of each regular issue of the PCT Gazette.*

**Published:**

— *with international search report*

## PERFORMANCE-BASED METHOD FOR OBTAINING SAVINGS IN AN INDUSTRIAL PROCESS

**PERFORMANCE-BASED METHOD FOR OBTAINING SAVINGS IN AN**  
**INDUSTRIAL PROCESS**

## BACKGROUND OF THE INVENTION

## 1. Field of the Invention

The present invention relates to a method for obtaining savings in an industrial process, and more particularly to a method for obtaining savings in the operating and/or fixed costs of an industrial process.

## 2. Description of the Related Art

Although owners and operators of industrial processes constantly look for ways to minimize processing costs and improve processing efficiency, their main focus is usually on maintaining production rate and quality to meet market demands.

Often they find it difficult to justify time and expense to analyze secondary, or collateral, problems, such as how to improve energy efficiency, use of labor, or the efficiency of use of consumables and raw materials and the like. Thus, opportunities for improvement in these collateral areas often are not sought. Moreover, even if these collateral opportunities are identified, capital and/or operating expenditures necessary for their implementation often cannot be justified in view of competing needs for capital that are more central to the operation of the process.

One option of the process owner for making improvements in collateral areas is to obtain the help of a third party. For example, a process owner can hire a consultant to analyze the process and identify opportunities for process savings. But

often the consultant's report to the owner is the only tangible result. The consultant's recommendations may or may not be implemented, and the risk of failure -- in addition to the cost of the consultant -- falls almost entirely upon the process owner. Similarly, asset-based lenders and general lending institutions can provide funds for 5 new equipment, but lack the expertise to analyze the process and select the most profitable modifications. In addition, they usually leave the implementation of the modification to the owner. Utility companies and equipment suppliers can provide expertise, equipment and financing, but only in their area of interest. Engineering companies have the skills to carry out the analysis, but require payment for their work 10 irrespective of its ultimate success. In consequence, many potential improvements to existing industrial processes go unidentified and unimplemented due to the lack of a method to align interests so that all of the participating parties benefit from the ultimate success of the project; the lack of a method that provides suitable and attractive incentive for all participating parties; the lack of a method that effectively 15 apportions risk of failure; and the lack of a method that permits the financing of capital expenditures off the balance sheet of the process owner.

Recently, private companies have been formed for the purpose of developing, installing and financing projects designed to improve the energy efficiency and reduce the maintenance costs for facilities. These companies, termed "energy service ① companies", or "ESCO's", typically contract with a host facility to survey opportunities for saving energy in areas such as high efficiency lighting, high efficiency heating and air conditioning, efficient motors and variable speed drives and centralized energy management systems. An unique feature of ESCO's is their provision of performance-based contracting, in which the ESCO's compensation for a 20 project, and sometimes the project financing, is directly linked to the amount of energy that is actually saved. More information on the subject of ESCO's and their operation can be found in the publication *What is an ESCO?* (available on May 21, 1999, at the website: [www.naesco.org](http://www.naesco.org)). Further information on the methods for measuring and verifying the energy savings that flow from ESCO projects can be 25 found in *Measurement and Verification (M&V) Guidelines for Federal Energy Projects*, a report prepared for ESPC Working Group, Federal Energy Management Program (FEMP), by Schiller Associates, Oakland CA, February 1996.

Thus far, the application of the methods used by ESCO's have been limited to the fields of lighting; heating, ventilating and air conditioning (HVAC); and the like and have not been applied to the more complex field of industrial processes. Even though a great deal of energy is consumed by industrial processes in the United States, the majority of ESCO's serve only the commercial and institutional -- rather than industrial -- markets. Lighting and HVAC in the commercial and institutional markets also consume a great deal of energy and are more visible to ESCO's, because of the far higher number of commercial and institutional installations. Thus, ESCO's have focused their efforts on the largest and most widespread market for their services -- lighting and HVAC. Another reason why the methods used by ESCO's have not been applied to industrial processes is the markedly greater complexity of an industrial process as compared with a lighting, or HVAC installation. This added complexity is indicated by the significantly larger number of independent variables that are present for industrial processes than are encountered in the less complex environmental systems. Techniques developed for measuring the savings resulting from modification to non-industrial applications cannot simply be applied to measure the savings that are the result of modifications of more complex industrial process systems, because the ESCO techniques lack sufficient accuracy and dependability when applied to complex industrial processes.

One example of a typical energy conservation system is described in U.S. Patent No. 4,990,893, to Kiluk, which discloses a method for an alarm system in which energy use in apartments and the like is monitored over a period of time to provide an average distribution pattern. Subsequent actual energy use is compared versus the average distribution pattern and an alarm is activated if the average and actual distribution patterns differ by a predetermined amount. In the method of Kiluk, time is the only independent variable that is considered and no provision is made for variations in environmental conditions, activity within the apartment, or other common variables that can affect energy use, but are independent of time. Thus, the method of Kiluk would result in an energy savings calculation of very low accuracy if applied to an industrial process having many independent variables such as processing rate, environmental temperature, type of fuel used, type of raw materials or reactants used, and the like. Accordingly, it would be useful to provide a method for measuring

energy use for an industrial process, specifically energy savings due to modifications or changes, which would take into account common independent variables.

Another example can be found in U.S. Patent No. 5,717,609, to Packa *et al.*, where a method is disclosed for measuring energy savings due to a retrofit of the type where some part of the baseline (non-retrofitted) environment is preserved and can be used to measure baseline energy transfer parameters. By simultaneously measuring heat transfer in the baseline environment and the retrofitted environment, the difference between the two indicates the savings due to the retrofit. However, the Packa *et al.* method cannot be used in situations where no part of the baseline environment can be preserved, such as, for example, with a change in fuel, or a change in energy transfer equipment, because there is no way to measure heat transfer in the baseline environment. Thus, it would be useful to provide a method that could monitor and report energy savings due to modifications or changes in the system or process of interest that do not preserve any part of the non-retrofitted, baseline, environment. Furthermore, it would be useful if the method could also determine and show the operating characteristics of the process -- such as whether the process was statistically in control and/or to define the trend in process productivity for the process.

The lack of an accurate method to measure the results of any modifications and to show the operating characteristics of the process on a real-time basis, limits the credibility between a party that might be best able to identify and implement a collateral improvement to an industrial process -- such as an independent contractor that specialized in such work -- and the process owner, who must authorize the modification. Without such credibility, the process owner is often hesitant to permit the contractor to enter its site; to obtain the data necessary for effective analysis and planning for modifications; and to design and implement the modification.

Industrial processes typically use the input of certain amounts of energy, labor, consumables, raw materials and the like to produce products at a certain rate. The amount of product that can be produced per unit of input is termed the "productivity" of the process. Productivity can be expressed on the basis of energy, labor, consumables, raw materials and the like, as mentioned above, but also on the basis of the amount of capital invested in the process, or on the size of the process equipment,

or even another basis. Since most industrial processes produce some type of product, the productivity can be expressed as, for example, number of units of product produced ("production") per unit of time ("production rate"). Common productivity parameters include production per unit of energy use, production per unit of labor, 5 production per unit of equipment size, production per unit of invested capital, and the like. An advantage of the parameter of productivity is that it permits one to measure the operating efficiency of the process as a function of some particular basis: *i.e.*, energy use, labor, consumables use, or the like. The inverse of the productivity function -- *i.e.*, energy use per unit of production --, or any parameter that is directly 10 or inversely related to productivity, would also serve the same purpose of measuring productivity.

Owners and operators of industrial processes compete with others who produce the same products and sell to the same market. It is important to minimize the cost of their process and products in order to improve their competitive position. 15 One method of reducing processing costs is by finding and implementing modifications to the process that increase the productivity of the process. An example can be provided by process energy use. Any modification to the process or its operation that reduces the amount of energy used per unit of production will improve the production per unit of energy use and, ultimately, can reduce the cost per unit of 20 product and place the owners and operators in a better position relative to their competitors. Since companies generally seek to maximize profitability, minimizing cost is a valuable means for accomplishing that end.

However, problems remain that hamper the efforts of industrial process owners in obtaining savings in their processes. Among these problems are the 25 difficulty in aligning the interests of participating parties so that they each benefited from the ultimate success of the project. Also remaining is the difficulty in providing suitable and attractive incentive for all participating parties and effectively apportioning the risk of failure. Adding to these difficulties is how owners can 30 finance the cost of improvements without including the debt burden on their balance sheets. Further, if another party is to be involved, the difficulty of how to systematically and accurately measure the added value that resulted from process improvements, rather than from changes in variables unrelated to the modification.

Furthermore, difficulty remains in how to provide the process owner with information that could be used in the management of the process as to whether the process was statistically in control and/or to define a trend in process productivity for the process.

#### BRIEF SUMMARY OF THE INVENTION

5        Briefly, therefore, the present invention is directed to a novel method for  
obtaining savings in an industrial process comprising the steps of establishing a  
10      performance-based contract between the owner of the industrial process and a  
contractor; deriving with a computer a statistical mathematical model that describes a  
productivity-related parameter for the industrial process in terms of independent  
15      variables; identifying a modification that will improve the productivity-related  
parameter; and implementing the modification.

Among the several advantages found to be achieved by the present invention, therefore, may be noted the provision of a method for obtaining savings in the operating and/or fixed costs of an industrial process that aligns the interests of  
15      participating parties so that they each benefit from the ultimate success of the project; the provision of such method that provides suitable and attractive incentive for all  
participating parties and effectively apportions the risk of failure among the parties; the provision of such method that permits financing of capital expenditures off the balance sheet of the process owner; the provision of such method that is capable of  
20      systematically and accurately measuring the savings that results from the  
modification, rather than from changes in variables that are unrelated to the  
modification; and the provision of such process that provides the process owner with information that could be used in the management of the process as to whether the process was statistically in control and/or to define a trend in process productivity for  
25      the process.

#### BRIEF DESCRIPTION OF THE SEVERAL VIEWS OF THE DRAWINGS

Figure 1 is a block diagram of one embodiment of the major steps in the method of the present invention;

30      Figure 2 is a block diagram of the steps for deriving a statistical mathematical model of the present invention;

Figure 3 is plot of the actual natural gas use for a steel works and the natural gas use as predicted by a statistical mathematical model of the present invention;

Figure 4 is a plot of the daily gas savings (predicted energy use - actual energy use) for a tube mill as a function of time; the plot also shows the variation in energy savings compared with 1, 2 and 3 standard deviations from the process average for the purpose of using the plot as a statistical process control chart; and

5 Figure 5 is a plot of actual and predicted natural gas usage as a function of time for a tube mill furnace showing the effect on energy usage of the implementation of a modification of the furnace control system.

#### DETAILED DESCRIPTION OF THE INVENTION

In accordance with the present invention, it has been discovered that savings 10 in operating costs from improved efficiency in energy use, use of consumables, production rate, and other productivity-related parameters and also savings in the fixed costs for an industrial process can be obtained by establishing a performance-based contract between the owner of the industrial process and a contractor. The performance-based contract provides for analyzing and improving the process and 15 binds the owner and the contractor with terms that provide the advantages of, for example, apportioning risks between the parties to the party best able to minimize each risk, and aligning the interests of both parties toward the success of the modification. After the contract is established, a statistical mathematical model is derived with a computer. The model describes a productivity-related parameter for 20 the industrial process in terms of independent variables. After the identification of a modification that will improve the productivity-related parameter, the contractor implements the modification.

It has been found that the feature of coupling the establishment of the performance-based contract with the derivation of a statistical mathematical model 25 that describes a productivity-related parameter for the process in terms of independent variables has the surprising advantage of building trust and credibility between the owner and the contractor. It is believed that this result occurs because the model provides an accurate and mutually-agreed-upon measure of the savings that result from the modification. Trust and credibility are major factors in obtaining the 30 authorizations and approvals that enable the desirable modification to occur, and without it, many useful and profitable modifications would not occur at all.

The statistical mathematical model is derived by using a computer. A key feature of the model is that it describes a productivity-related parameter in terms of independent variables; preferably, in terms of a validated set of independent variables (as those terms are defined below). After a modification to improve the productivity 5 of the process is identified and implemented, the change in the productivity-related parameter caused by the modification is measured by determining the difference between a measured value of the parameter and a value of the parameter predicted by the model using measured values of each independent variable. If desirable, a value can be assigned to the change in the productivity-related parameter, and the savings 10 achieved by the modification can be shared between the owner and contractor.

The present invention has been found to be particularly useful for application to industrial processes that consume energy and other consumables during the transformation of raw materials to a finished product. As used herein, an "industrial process" is distinguished from an HVAC, or a lighting system, or a small collection of 15 simple devices such as pumps and the like, on the basis that in the industrial process, most of the energy that is used by the process is used to carry out the transformation of raw material to product, rather than used to control environmental conditions.

The typical industrial process is composed of one or more unit processes that are combined into a system within which the transformation takes place. It is more 20 common that the industrial process includes more than two or three unit processes and often includes over ten, or more. Depending upon the type of industrial process, these unit processes can be, for example - but without limitation: furnaces, molding systems, mixers, pelletizers, mills, grinders, heat exchangers, presses, distillation columns, reactors, boilers, filters, waste treatment systems, and the like. It is common 25 for the unit processes to be combined by interconnecting them with pipes, hoses, conveyors, slides, and the like, to form a complete and interconnected process for the transformation of a raw material to a finished product.

The industrial process can be owned by an owner and operated by an operator and, in many cases, the owner and the operator are the same entity. As used herein, 30 the term "owner" is meant to include both the owner and/or the operator of an industrial process. Unless specified otherwise, the steps of the subject method can be performed by the owner or by a contractor. When the steps are carried out by a

contractor, it is preferred that the contractor is unrelated to the owner in a legal sense, but is preferably an independent contractor. It is also preferred that the contractor have engineering skills, and more preferred that the contractor have engineering, management, consulting and industrial development investing skills. As will become 5 apparent, it is an advantage that the contractor perform some of the steps of the subject method. When a contractor is involved in carrying out one or more of the steps of the subject method, the owner may be termed the "client".

While the relationship between the owner and the contractor is not legally a partnership, it is believed that successful implementation of the subject method 10 benefits when each party fulfills its respective role. The contractor works with the client to conceive, plan, develop, fund, implement and maintain a process modification that results in savings. The owner provides access to personnel and data, authorizes expenditures and changes to its process, operates the modified process and shares the savings that result from the modification with the contractor.

15 Among the advantages of having an independent contractor perform some or all of the steps of the subject method is that an independent contractor can bring increased objectivity and new communication channels to the work. Moreover, as described above, process owners often cannot justify the time and/or expense of making improvements that are collateral to their main manufacturing business.

20 Furthermore, if the contractor is financially independent of the owner, it can borrow funds without affecting the balance sheet of the owner. Thus, participation of a contractor, having as its primary task the design, financing and implementation of such energy-saving projects, advantageously permits owners to undertake such improvements and to enjoy the benefits.

25 Establishing a performance-based contract

The performance-based contract of the present invention is a contract having at least the owner and the contractor as parties and that defines the respective duties and responsibilities of each party with respect to making modifications to obtain savings in an industrial process or plant. When it is said that the contract is "between 30 the owner and a contractor", it is to be understood that, although at least those two parties are included, other parties could also be included in the same contract.

It is preferred that the contract provides that the contractor will finance at least part of a modification that will improve a productivity-related parameter of the process, and that the contractor will implement the modification. It is believed that when the contract provides such terms, it serves to apportion the risk of failure

5 between the owner and the contractor and assigns primary responsibility for the success of each step of the modification to that party most capable of controlling its success. For example, since the contractor has expertise in finding and designing technical modifications and installing and starting up new or modified equipment, those tasks are assigned to the contractor. As another example, since the owner has  
10 greater access to historical process operating data and to personnel with experience in operating the process, the responsibility for providing access to data and to experienced operating personnel is assigned in the contract to the owner.

It is also preferred that the contract provides that the owner will share the savings that result from the improvement with the contractor. It is believed that by

15 paying the contractor from the actual savings achieved by the modification, the interests of both the owner and the contractor in the success of the modification can be aligned. It is thought that this advantageous alignment minimizes friction between the parties and makes it more probable that a decision by one party will be in the best interests of the other party.

20 It is more preferred that the performance-based contract also provides that the owner and the contractor agree on the model prior to the implementation of the modification; and even more preferred that the contract also provides that the contractor has sufficient authority to manage the implementation of the modification. It is believed that by reaching agreement on the model(s) that describe one or more of  
25 the productivity-related parameters of the process prior to implementing a modification, the parties establish a strong basis for mutual trust and credibility. Whereas, if the modification were to be implemented prior to such agreement, more opportunities for misunderstanding and disagreement could arise. It is also believed that when the contract provides the contractor with sufficient authority to manage the  
30 implementation of the modification, the risk of failure is reduced. When it is said that the contractor has "sufficient authority to manage the implementation of the modification", what is meant is that the contract provide that the contractor can have

its own personnel on the plant site; that the contractor can schedule activities of the modification; that the owner will provide the contractor access to its operating personnel for strategy team-building and implementation of the modification; that the owner will provide the contractor access to historical operating data; and that the 5 contractor can subcontract various portions of the modification to subcontractors and can control the activities of those subcontractors.

Although the performance-based contract can be for any length of time, it is preferred that the term is long enough to permit full planning, implementation and 10 operation of the modification and also long enough to provide for the repayment of borrowed funds and for the agreed-upon sharing of savings. A term of about 24 months is often sufficient, but longer terms are sometimes desirable.

#### Deriving a Statistical Model

One step of the present method is to derive a statistical mathematical model that describes a productivity-related parameter for the industrial process in terms of 15 independent variables. It is preferred that the independent variables form a validated set of independent variables. As used herein, the terms "statistical mathematical model" refer to a model that is a best-fit model for a given set of data. Due to the large amount of data that must be gathered and processed in order to effectively model an industrial process, it is preferred that the derivation of a model be carried 20 out by a computer. Once the model has been derived, it can be applied by hand calculations. However, it is preferred that the application of the model is also carried out by a computer in order to increase the speed and accuracy of computation.

As discussed previously, the productivity of an industrial process can be expressed on the basis of time, energy use, consumables use, labor, the amount of 25 capital invested in the process, or on the size of the process equipment, or other basis. Productivity per unit time is often expressed as, for example, number of units of product produced ("production") per unit of time ("production rate"). Other productivity parameters include production per unit of energy use, production per unit of labor, production per unit of equipment size, production per unit of invested 30 capital, and the like. The inverse of the productivity function -- *i.e.*, energy use per unit of production --, or any parameter that is directly or inversely related to productivity, such as energy use per unit period of time, will serve the same purpose

of measuring productivity and can act as the productivity-related parameter. As used herein, the term "productivity-related parameter" is to be understood to include all commonly-used productivity parameters -- including those listed above; the inverse of those conventional parameters; and all parameters that are inversely or directly related thereto. Thus, energy use per unit time, consumables use per unit time, or production per unit of time, are to be considered to be included as productivity-related parameters.

For the purpose of example, some of the description of the subject method herein will be in terms of productivity on the basis of energy (production per unit of energy use), or of the inverse parameter -- energy use per unit of production, or energy use per unit of time. However, it is to be understood that when energy use is used as an example, similar methods and equations could be derived for any other productivity-related parameter, simply by substituting the appropriate variables and parameters.

Industrial energy consumption is a function of numerous contributing factors, caused by equipment that uses energy in response to demands placed on it by the user and according to its particular design. Energy efficiency improvements usually concentrate on individual parts or systems, while overall energy consumption is often analyzed by examining the use of energy in its specific fuel forms. Because independent variables affect consumption of these fuels, accurate comparisons of the energy consumption for time measured periods for a process must include the effect of each of these variables.

Reductions in industrial energy consumption typically result in energy cost reductions. However, it should be recognized that energy cost can also be reduced by using energy at alternative times (e.g., by using electricity during "off peak" hours), using alternative forms of energy (e.g., fuel switching), or negotiating more favorable utility rates. The contractor can implement cost-effective scheduling of energy use and fuel switching and may assist the owner in negotiating for more favorable rates for the purchase of energy and power.

In many cases, it is possible to determine the quantitative effects of one or more of the independent variables through a statistically valid regression analysis of historic data for the process. The regression model may be linear, or may be

dependent upon other functions such as powers, time lead or lag, codependency or exponentials. The most common model is linear, but other dependencies are sometimes encountered.

The inventors have found that it is preferred to use a statistical mathematical model to predict and track energy performance for an industrial process for several reasons. First, the model can be used as a basis for measuring energy savings and for determining the share of savings that should go to the owner and to the contractor. Second, the model can be used as a valuable management tool for reducing energy costs on a day-to-day basis. And, third, the model can serve as a standard against which trends in the process' performance can be measured.

The modeling process includes the systematic identification of all of the special or assignable causes of variability in energy use and defining the contribution of each to changes in energy use. For example, it is intuitively known that energy use will generally increase when production rate increases, and that relationship should be built into the model by using a production rate coefficient(s). An accurate, reliable and repeatable model depends upon inclusion of all of the assignable causes of variation in energy use. One preferred characteristic of the validated set of independent variables of the present method is that the set includes all independent variables necessary to identify all of the special or assignable causes of variability for the process.

Models of energy usage, or of any other productivity-related parameter, are developed using the statistical technique of multiple linear regression. The use of multiple linear regression analysis for the derivation of mathematical models is well known and additional information can be found in *Introduction to the Practice of Statistics*, by David S. Moore and George P. McCabe, W. H. Freeman & Co. (1989); and *Statistics*, by David Freeman, *et al.*, Second Ed., W. W. Norton & Co. Among the assumptions on which the multiple linear regression method depends are that a linear relationship exists between the independent variables and the dependent variable; the variables are normally distributed; and the observations used in the calibration sample are independent. The assumptions of linearity and normality should be addressed by standard statistical tests and, if necessary, data

transformations or smoothing techniques, as described in the references cited above, may be used to compensate for some instances of non-linearity and abnormality.

Some of the key steps that are used for the derivation of a statistical mathematical model that describes energy use per unit of production in terms of 5 significant independent variables are shown in Figure 2. It should be understood that the same method can be used for the derivation of a model for any productivity-related parameter, merely by substituting the appropriate dependent and independent variables. The overall process for deriving the model can be described as follows:

The industrial process that is to be modeled is identified and, preferably, a 10 flow chart is constructed of the entire process. The flow chart should indicate main energy sources for the process, such as electricity, coal, oil, gas, water, steam, and the like. The chart should also indicate the products produced and, preferably, the volume of product(s) that is produced per unit time. It is also useful if the chart identifies energy consumption measurement points for the process; *i.e.*, where and 15 how energy use is measured.

Unit processes are selected and defined that will be segmented from the industrial process for modeling purposes. The unit processes, as described previously, are processing units that have been combined together to make up the process. The following steps are then carried out for each of the unit processes.

- 20 1. The individual fuel forms/energy sources to be modeled (predicted) are identified.
2. Whether energy sources are to be treated independently or whether there are substitutions (*i.e.*, alternative fuels like coke oven gas and natural gas) that must be modeled together, is decided. It is preferable to derive a separate model for each fuel 25 source that is used in the unit process (*i.e.*, natural gas, coal, steam, electricity, etc.) unless some internally-generated material (such as coke oven gas or refining light ends) is substituted in whole or in part for another external source of energy (such as natural gas), in which case, it is preferable to include both fuel sources in the same model.
- 30 3. Independent variables are identified for testing as potential members of the validated set of independent variables (e.g., production quantities, degree-days, production days, office days, days of the week, product mix, and the like). The

criteria for inclusion and testing are that the independent variable be one that could potentially have an effect on the dependent variable (energy consumption) in the unit process and that sufficient data exists to test the validity of the variable. Historical data is collected for energy consumption and for each of the independent variables.

5     Although monthly readings/records for two years can be used to test the variables, it is preferred that the data collected represent at least two years of daily readings and/or records, and to have been recorded since any major process change. It is more preferred that the data collected represent at least three years of daily readings and/or records, and to have been recorded since any major process change.

10    . 4. All of the potential independent variables that were identified in step 3 are organized into a database with one column (field) assigned to each variable, and one row (record) assigned to each daily or monthly reading. All independent variables for which data are available are incorporated into the database. It is preferred that from about 50 to about 150 independent variables are identified and included in the

15    database. In order that the resulting analysis provides a model in which high confidence can be placed, it is preferred that there are more rows than columns in the database by a factor of about 10. For 100 independent variables, for example, this would require about 1,000 days of data -- or the equivalent of about three years of operating data.

20    5. The data is separated into two portions -- one portion to be used for the derivation of the mathematical model (the correlation data) and another portion to be used for verification of the accuracy of the model (the validation data: preferably data from the most recent 2 - 3 months).

25    6. Using a computer, a regression analysis is performed using the correlation data for the dependent energy use variable versus the selected independent variables to obtain a regression model that describes the energy use for the unit process in terms of the selected independent variables, regression coefficients and constants. For each unit process, this model can have the form:

$$30 \quad E_k = r_{Bk} + \sum_{j=1}^i r_{kj}(V_j)^m$$

where:

$E_k$  is the energy use for the  $k^{\text{th}}$  unit process per unit time;

$r_{Bk}$  is a constant representing the base energy load for the  $k^{\text{th}}$  unit process per unit time;

$V_j$  is the  $j^{\text{th}}$  significant independent variable for the  $k^{\text{th}}$  unit process;

$r_{kj}$  is the linear regression coefficient for the  $j^{\text{th}}$  independent variable in the  $k^{\text{th}}$

5 unit process that provides the best fit in a correlation of the effects of  $V_j$  upon  $E_k$  as determined by multiple regression analysis of historical data;

$m$  is a best fit constant correlating the effect of  $V_j$  upon  $E_k$  as determined by multiple regression analysis of historical data and is a fraction or whole number from 0 to about 3;

10  $j$  is a number designating one of the significant independent variables in the  $k^{\text{th}}$  unit process and is an integer from 1 to  $i$ ; and

$i$  is that number of significant independent variables in the  $k^{\text{th}}$  unit process that comprise a set of significant independent variables for that process.

15 It is preferred that  $m = 1$ , and that linear equations are statistically adequate to describe the relationship between the dependent variable and the independent variables.

It is believed that the regression analysis can be performed on any computer that has a processor that operates at a speed and capacity equal or better than that of an Intel™ 486 processor operating at 33 Mhz speed. However, it is preferred that a 20 computer having a Pentium™ 100 processor, or faster processor, is used. The computer should be programmed with a regression analysis software program. The regression analysis that is available in, for example, Lotus™ 1-2-3, version 5.0, or newer; or in Excel™, version 5.0, or newer; or in SAS, version 6.12, or newer; is suitable for the derivation step of the present method.

25 7. The value of the ratio of each coefficient to the standard error of the coefficient is determined. If this value is close to zero, the variable corresponding to the coefficient is not a significant variable and should be dropped from the model. To determine whether a coefficient is "close to zero", the value of the ratio of the coefficient divided by its standard error is compared with tabulated values in a t-test 30 (as described, for example, in *Introduction to the Practice of Statistics*, by David S. Moore and George P. McCabe, W. H. Freeman & Co. (1989)). As a rule of thumb, if

the value of such ratio is greater than 2 in magnitude, the variable is a significant variable and should be maintained in the model.

8. The predictive ability of the regression model is checked by testing its ability to predict the energy use for the validation data set. As used herein, this predictive ability of the model will be termed the "accuracy" of the model. The accuracy of the model is determined by calculating the percent deviation between the actual and predicted energy use on a daily, monthly, or yearly basis -- depending upon the type and amount of validation data that is available. The percent deviation is calculated as follows: the actual use of energy for a period (e.g., 1 day) is subtracted from the energy use predicted by the model. This difference is divided by the predicted use and multiplied by 100 to obtain the percent deviation for that period. For the calculation of the average deviation over multiple individual time periods (e.g., one month of 30 days) the absolute value of the deviation,  $|D|$ , for each day is summed over the multiple time periods, divided by the sum of the daily predicted values and multiplied by 100.

The model is tested for predictive accuracy as follows: If the monthly deviation is less than  $\pm 5\%$  and the yearly deviation is less than  $\pm 1\%$ , the model is accepted. If the monthly deviation is more than  $\pm 5\%$ , or the yearly deviation is more than  $\pm 1\%$ , the model is rejected. If the model is rejected, one or more additional independent variables for the unit process are identified and selected as described in step 3 and derivation and testing of the model is repeated from step 3 until the model meets the predictive accuracy tests described herein.

9. At this point, it is preferred that the model is reviewed with the owner and/or operator of the process for input and qualitative validation.

10. The predicted energy use values and the actual energy use values is preferably plotted versus time in calendar sequence and the resulting plot examined to identify any trend or step-change variations in the predicted versus actual energy values over time. If a trend or step-change deviation of actual versus predicted energy use is apparent, the historical data should be corrected by eliminating data prior to the trend or step-change. The complete regression analysis should be re-run from step 3, using the new, limited data set.

11. The assumption of a linear relationship between each independent variable and the dependent variable (energy use, in this example) is checked by sorting the data by each independent variable in turn and analyzing for any patterns or trends in the deviation between actual and predicted value of the dependent variable.

5     If there is a trend, a multi-part model should be constructed such that the pattern or trend is fit by the new, multi-part model. The coefficients for each independent variable in each model are compared to see if they are significantly different for the several parts and whether the fit is significantly improved by using the multi-part model. If the fit is significantly better for the multi-part model, the multi-part model

10    should be used, rather than the one-part model.

12. The validation data should be inspected for outlying data points -- data points that are more than 3-times the standard error of estimate away from the prediction. If any outlying data points are identified, explanations should be sought for the outlying data points and such data points should be eliminated from the

15    database only after failure to correct the data point to a value within 3-times the standard error by checking it against all other records and/or information tending to indicate the true value of the data point (*i.e.*, source documents, memories of operating personnel, operating logs, comparison with other values of the same variable with other points that have similar operating conditions affecting energy use,

20    or the like);

When all energy sources have been modeled for every unit process, all of the unit process models can be incorporated into a model that describes the energy use for the total industrial process per unit of production in terms of significant independent variables. The overall model of the process productivity on the basis of energy use

25    can have the form:

$$\underline{P_E = P_T/E_T}$$

where,

$P_E$  is the production of products per unit of process energy use;

$P_T$  is the production of products from the process per unit time; and

30     $E_T$  is the energy used by the process per unit time.

and where,

$$E_T = r_B + \sum_{k=1}^n E_k$$

where:

5             $E_T$  is the energy use for the total industrial process per unit time;

10           $r_B$  is a constant representing the base energy load for the total industrial process per unit time;

15           $n$  is the total number of unit processes in the industrial process;

20           $k$  is the identifying numeral for one of the  $n$  unit processes and is a positive integer from 1 to  $n$ ; and

25           $E_k$  is the energy use for the  $k^{\text{th}}$  unit process per unit time.

The terms  $r_B$  and  $r_{BK}$ , which describe the base energy load for the whole industrial process and the base energy load for one of the unit processes comprising the industrial process, respectively, are defined during the multiple regression model derivation and represent that part of the energy use rate that would be expected if the 15 value of each of the significant independent variables was zero.

In cases where it is desirable to use the production rate ( $P_T$ ) as an independent variable, one can simply use the total energy use of the process per unit time ( $E_T$ ) as the productivity-related parameter.

20          Likewise, a model of production per unit of time (production rate) can be derived that is of the form:

$$P_T = s_B + \sum_{k=1}^n P_k$$

where:

25           $P_T$  is the production for the total industrial process per unit time;

30           $s_B$  is a constant representing the base production for the total industrial process per unit time;

35           $n$  is the total number of unit processes in the industrial process;

40           $k$  is the identifying numeral for one of the  $n$  unit processes and is a positive integer from 1 to  $n$ ; and

45           $P_k$  is the production for the  $k^{\text{th}}$  unit process per unit time, and can be represented by a formula having the form

$$P_k = s_{Bk} + \sum_{j=1}^m s_{kj}(U_j)^m$$

where:

$P_k$  is the production for the  $k^{\text{th}}$  unit process per unit time;

5  $s_{Bk}$  is a constant representing the base production for the  $k^{\text{th}}$  unit process per unit time;

$U_j$  is the  $j^{\text{th}}$  significant independent variable for the  $k^{\text{th}}$  unit process;

10  $s_{kj}$  is the multiple regression coefficient for the  $j^{\text{th}}$  independent variable in the  $k^{\text{th}}$  unit process that provides the best fit in a correlation of the effects of  $U_j$  upon  $P_k$  as determined by multiple regression analysis of historical data;

$m$  is a best fit constant correlating the effect of  $U_j$  upon  $P_k$  as determined by multiple regression analysis of historical data and is a fraction or whole number from 0 to about 3;

15  $j$  is a number designating one of the significant independent variables in the  $k^{\text{th}}$  unit process and is an integer from 1 to  $i$ ; and

$i$  is that number of significant independent variables in the  $k^{\text{th}}$  unit process that comprise a set of significant independent variables for that process.

20 It is preferred that  $m = 1$ , and that linear equations are statistically adequate to describe the relationship between the dependent variable and the independent variables.

In like manner, if the productivity-related parameter is consumables use per unit time, a model can be derived of consumables use per unit of time having the form:

$$25 C_T = t_B + \sum_{k=1}^n C_k$$

where:

$C_T$  is the consumables use for the total industrial process per unit time;

30  $t_B$  is a constant representing the base consumables use for the total industrial process per unit time;

$n$  is the total number of unit processes in the industrial process;

$k$  is the identifying numeral for one of the  $n$  unit processes and is a positive integer from 1 to  $n$ ; and

$C_k$  is the consumables use for the  $k^{\text{th}}$  unit process per unit of time, and can be represented by a formula having the form:

$$5 \quad C_k = t_{Bk} + \sum_{j=1}^i t_{kj}(W_j)^m$$

where:

$C_k$  is the consumables use for the  $k^{\text{th}}$  unit process per unit time;

$t_{Bk}$  is a constant representing the base consumables load for the  $k^{\text{th}}$  unit process per unit of time;

10  $W_j$  is the  $j^{\text{th}}$  significant independent variable for the  $k^{\text{th}}$  unit process;

$t_{kj}$  is the multiple regression coefficient for the  $j^{\text{th}}$  independent variable in the  $k^{\text{th}}$  unit process that provides the best fit in a correlation of the effects of  $W_j$  upon  $C_k$  as determined by multiple regression analysis of historical data;

$m$  is a best fit constant correlating the effect of  $W_j$  upon  $C_k$  as determined by

15 multiple regression analysis of historical data and is a fraction or whole number from 0 to about 3;

$j$  is a number designating one of the significant independent variables in the  $k^{\text{th}}$  unit process and is an integer from 1 to  $i$ ; and

20  $i$  is that number of significant independent variables in the  $k^{\text{th}}$  unit process that comprise a set of significant independent variables for that process.

It is preferred that  $m = 1$ , and that linear equations are statistically adequate to describe the relationship between the dependent variable and the independent variables.

25 It should be understood that any one of these models or any combination of two or more of these models can be, and often are, used to describe the changes in various productivity-related parameters for the same process. When a computer is used to calculate the predicted values of each of the dependent variables, they can easily be calculated and reported at any time that the values of the significant independent variables for all of the models are measured.

30 One important consideration of a model is its validity as a predictive tool. It is important that the model measures and models what it is intended to measure and model, rather than to be simply a good fit of past data. Testing the accuracy of the model is described in step 8, above. The inventors believe that it is preferable to

require that the model conform to the standards of accuracy described in step 8, for several reasons. First, the more accurately the model predicts the productivity-related parameter, the less "noise" there is in the calculated values and the easier it is to notice and identify special causes of variation in the process (causes that are not caused by 5 changes in the independent variables) and to take timely corrective action. Second, if the model is to be used as the basis for calculating the amount of energy savings that is actually being achieved, all parties involved can proceed with a higher level of confidence when the model meets the required accuracy standards.

It is also important that the model truly measures the changes in the 10 productivity-related parameter that are caused by changes in the independent variables. This quality can be measured by calculating the correlation coefficient (R). Statistical parameters, such as the value of R-squared (or,  $R^2$ ), are measures of the degree of change in the dependent variable (the productivity-related parameter) that is explained by changes in the independent variables that have been selected for the 15 model. It is believed that if R-squared is lower than 0.6, then it is likely that the model will not accurately predict values of energy use. The advantage gained from having a model that fully explains all, or most, of the degree of change in the dependent variable as a function of changes in the independent variables is that it provides a higher confidence level that the changes predicted by the model truly 20 reflect the change caused by known events. For the purpose of the present invention, it is preferred that the value of R-squared be not under 0.7, more preferred that R-squared be not under 0.8, and yet more preferred that the value of R-squared be not under 0.9.

The inventors also believe that it is important to ensure that co-linearity 25 diagnostics are carried out on the independent variables in order to identify and eliminate any possible co-variance problems. Two common methods that can be used for this purpose are found in the statistical analysis program, SAS. Those methods are: (1) a direct method in which, with the dataset open in "Statistical Analysis" mode, the "Statistics, Descriptive, Correlations" test can be used to review correlations 30 between independent variables; and/or (2) a linear regression method, through which a "Correlation Matrix of Estimates" and/or "Covariance Matrix of Estimates" can be selected under the "Statistics" tab in the Linear Regression "Statistics" dialog box. In

both methods, the resulting output is a covariance matrix that can be interpreted to determine the existence of co-linearity of the independent variables. It is preferred that co-variate independent variables are eliminated from the model.

Another way to validate a model is to apply the model to future observations 5 during a test period. In other words, to predict the energy use for each day based on the values of the significant independent variables for that same day and then to compare the predicted value with the measured value of energy use. If this can be done over a test period of several months, a good check of the validity of the model can be obtained. However, this method obviously requires additional time for model 10 verification -- time that could otherwise be used to improve and benefit from the productivity of the process. Therefore, a preferred method for validating the model is to withhold a portion of the historical data as a validation sample. Then, as described above, a model that was derived on the basis of calibration data can be validated for accuracy by testing its predictive accuracy versus the data of the validation sample.

15 As mentioned above, it is an important feature of the present invention that the model describes the dependent variable in terms of independent variables. It is preferred that the independent variables that appear in the model form a validated set of independent variables. As used herein, the terms "validated set of independent variables" refer to a set of independent variables that provides a mathematical model 20 that meets the accuracy tests described in step (8). It is preferred that the validated set of independent variables also includes no unexplained trend or step-change variation as described in step (10); provides a mathematical model that has an  $R^2$  value (determined as described above) of not less than about 0.6; and is free of co-variance 25 (as described above). It is preferred that the validated set of independent variables further provides a model that has an  $R^2$  value of not less than about 0.7; more preferred that the validated set of independent variables further provides a model that has an  $R^2$  value of not less than about 0.8; and even more preferred that the validated set of independent variables further provides a model that has an  $R^2$  value of not less than about 0.9.

30 If an independent contractor has derived the model, it is preferred that the model is presented to the process owner and/or operator for approval prior to proceeding further with the identification and implementation of changes to improve

productivity. Thus, after verification of the model is completed satisfactorily by the contractor, the model is presented to the process owner and/or operator for approval. If the model is not approved, the model derivation process is preferably begun again at step 3, described above. This iteration is repeated until the model is approved by 5 the owner.

#### Identifying Modifications to Improve Productivity

One embodiment of the subject method is to identify and implement some type of modification to the process that will improve the productivity of the process. As described above, the productivity of the process is measured, at least in part, by the 10 measurement of a productivity-related parameter. As used herein, the terms "improve the productivity-related parameter" are to be understood to mean a change in a productivity-related parameter that would result in a process change that the owner would find desirable. For example, a decrease in the cost per unit of product, an increased production rate, improved product quality, or reduced emissions, would all 15 be improvements in productivity-related parameters.

It is not critical how modifications to improve productivity of the process are identified and modifications can be identified by using standard industrial engineering methodology (e.g., short interval scheduling, audits, observations of the process, load calculations, inventory analysis, and other techniques). It is preferred that the 20 modification be one that can be made without affecting any independent variable that is included in the validated set of independent variables that appear in the model. When it is said that the modification does not affect such independent variable, what is meant is that the modification itself does not direct that a change be made in one of the independent variables. By way of example, if one of the independent variables in 25 a model of a chemical process is the operating temperature of a reactor, then a modification that proposed changing the reactor temperature would affect the independent variable. This is undesirable because the effect of the modification would be reflected in the predicted value of the productivity-related parameter as well as in the actual measured value. One way to handle such a situation is to remove the 30 affected independent variable from the model. Another way would be to insert a separate term in the model that corrected for any change in the predicted value caused by a change in the particular independent variable.

The modification of the present invention can be any type of modification that will result in an improvement in the productivity of the process. For example, the modification can be in how the process is operated (operational); in how and when the process and process-related equipment is maintained (maintenance); or in the actual equipment used in the process (equipment). Some examples of operational modification (without meaning to be limiting) are a change in a type of raw material or other consumable used; change in a type of fuel used; change in a process variable set point (*i.e.*, raise or lower temperature or pressure); or change in the speed of operation of the process, or a unit process. Some examples of maintenance modifications are changes in when the process is shut down for regular maintenance; or what maintenance is carried out when the process is down. Some examples of equipment modifications are substitutions of newer, more efficient process equipment for older, less efficient, equipment; enlargement or reduction of size of equipment; or addition or deletion of equipment.

One preferred method for identifying a modification to improve the productivity of the process is to use the validated and approved process model in a process simulation mode to test the desirability of various potential modifications. In this method, the model is used to predict productivity improvements (energy savings, for example) that would be obtained as a result of various modifications by simulating the results of proposed modifications of the equipment, materials and/or processing techniques of the process; calculating the cost-effectiveness of each such simulated modification; and comparing the cost-effectiveness of each such modified process with that of the unmodified process. At least one of the simulated modifications found to be cost-effective can then be selected for implementation. Various proposed modifications can even be tested and ranked in order of cost-effectiveness for consideration by management and/or sources of financing.

Other management considerations for ranking proposed modifications can include estimated speed of implementation, collateral benefits, ease of completion and acceptability of the modification to operating personnel.

**30 Implementing the Modification**

Any modification that has been selected as being one that is cost-effective and one that will produce an improvement in productivity can be implemented by any

party. It is preferred, however, that the implementation be done by either the owner, or by an independent contractor. It is more preferred that the modification be implemented by the contractor and that the contractor is the same entity that carried out the analysis and modeling of the process, and even more preferred that the 5 contractor was involved in the identification and selection of potential modifications. An advantage of having the contractor implement the modification is that the contractor is free of the responsibility of operating the process and running the plant, in general. Thus, the contractor can focus all of its energies upon the rapid and accurate design, ordering, construction, shake-down, testing, and start-up of the 10 process after the modification.

At this point, it is preferred that the risk is shifted to the contractor for achievement of the financial objectives and performance of the modification, and for the provision of accountability for its success. To insure the success of the modification, it is preferred that the contractor monitors the performance of the 15 process daily, builds teams between the contractor and owner personnel, holds daily team meetings, builds a management system for the operating perspective and trains the owner personnel to maintain the process.

#### Financing the modification

When the contractor makes the modifications, the cost of the modifications 20 can be borne by either the owner or by the contractor. It is preferred, however, that the contractor bear at least some part of the cost of implementing the modification, or modifications. It is more preferred that the contractor bear at least a substantial part of the cost of implementing the modification, and even more preferred that the contractor bear all of the cost of implementing the modification. This is believed to 25 be advantageous because the contractor has carried out the analysis and modeling of the process, and has participated with the owner in the identification and selection of cost-effective modifications to the process, and it is in the best position to know the risks of the modification project and to guard against financial loss that could be caused by such risk. When the modification is one that affects process operation or 30 maintenance, it is preferred that the contractor obtain the financing and bear substantially all of the costs associated with implementing the modification. When o the modification involves the purchase, installation and use of capital equipment, it is

o preferred that the contractor obtain financing for purchase of the capital equipment, purchase the capital equipment and act as the initial sole owner of record for the capital equipment.

It is believed that there are several advantages that may be gained when the  
5 contractor finances the purchase and installation of capital equipment. The equipment cost can be shown on the balance sheet of the contractor rather than the balance sheet of the process owner. This provides the advantage of allowing the owner to proceed  
0 with modifications, which may be highly cost-effective, but are secondary to the primary business of the owner and may be difficult or impossible to justify on the  
10 owner's own balance sheet.

The contractor preferably finances the purchase and installation of capital equipment by borrowing funds from a lender. This loan can be of any form that meets the specific needs of the owner and the contractor. It is preferred, however, that the loan is a general obligation loan and more preferred that the loan is a general  
15 obligation, non-recourse loan. As will be described in more detail below, it is  
o preferred that the loan be repaid entirely, or in part, from the savings that result from  
the modification of the process. Such savings can come from energy savings,  
increased production rate, reduction in the use of labor or consumables,  
environmental benefits, quality improvements, or any other measurable value-added  
20 benefits caused by the modification.

Moreover, if the contractor provides such financing for capital equipment for at least two or more separate owners, the contractor can spread the risk of loss for the contractor and the lender by obtaining the financing required for all of the capital equipment required in all of the projects under a loan to the contractor.

25 It is believed that this method of financing provides surprising advantages over conventional loans to the owner for which the capital improvement is carried by the owner on its balance sheet. By way of contrast, in the present method it is preferred that the contractor owns the asset and carries it on its balance sheet. By such means, termed "off-balance sheet financing", or "performance-based financing",  
30 the owner can keep the resulting capital assets and associated debt burdens off its balance sheet, thereby tapping a new source of capital to fund improvements and strengthen its own financial position from the savings generated from the capital

improvement. It is preferred that the loan is secured by a general obligation by the contractor, and more preferred that the loan is secured by a security interest in the asset. As described previously, such off-balance sheet financing for the owner permits the implementation of energy-saving modifications that it otherwise could not

5 undertake due to financial limitations.

It is also desirable to train the operating personnel of the process owner to use and maintain the new equipment, or newly modified operational practices for the process. Because the contractor has been involved in the selection, installation, start-up and initial operation of the equipment and/or operational modification, it is

10 preferred that the contractor provide training of the owner's personnel.

Upon the completion of the process modification, the process is started up and operated with the modification(s), thereby obtaining the benefits of the productivity improvements that result from the modification(s).

#### Measuring Savings Caused by the Modification

15 After the modification(s) has been implemented, it is necessary to measure the change in the selected parameter caused by the modification in a manner that will distinguish the effects of the modification from effects caused by other reasons. This is preferably done by determining the difference between a measured value of the productivity-related parameter and a value of the same parameter predicted by the

20 model using measured values of the one or more independent variables.

The model can be used to measure energy savings due to a modification in the operational practice, maintenance, or equipment of the process. This is done by measuring the actual value of the energy use, energy use rate, or parameter that is proportional to either of these, for the process (the "actual energy use"), and -- at the

25 same time -- measuring the actual values for all of the independent variables that appear in the energy use model. The values for the independent variables are used with the model to calculate a predicted energy use that the process would have experienced without the modification (the "predicted energy use"). The energy

30 savings is calculated by comparing the actual energy use with the predicted energy use. The difference between the two indicates the energy savings due to the modification (the "energy savings").

As mentioned previously, the same approach can be used to calculate the improvement in any productivity-related parameter simply by substituting appropriate parameters for energy in the method described above. By way of example, the savings in consumables use can be measured as:

5 (predicted consumables use) - (actual consumables use) = savings in consumables use  
or, the savings due to increased production rate can be measured as:

(actual production rate) - (predicted production rate) = increase in production rate

In case any of the calculated values result in negative numbers, the negative numbers can simply be used as is. For example, negative savings can be plotted on a graph as  
10 negative numbers.

#### Payment for the modification and sharing of savings

One feature of the present method is that payment of the cost of the modification, including the repayment of any loan for the purchase and installation of capital equipment, is to come from productivity improvements due to the  
15 modification. It is preferred that such costs are at least partly met by savings derived from the modification (for example, at least about 50% of the costs); more preferred that such costs are at least substantially derived from the modification (for example, at least about 75% of the costs); and most preferred that such costs are derived solely from the modification. When the terms "savings derived from the modification" are  
20 used, what is meant is the savings or increased profits, expressed in terms of money, that accrue to the process as a result of the modification. By way of example, these could be energy savings, savings in the amount and type of raw materials or consumables, or labor, increased production rate, environmental benefits, quality improvements or the like.

25 It is the intent of the novel method that not only the costs of the modification are met solely by savings derived from the modification, but that the savings actually exceed the costs. The excess of the savings over the costs of the modification represent the economic incentive to both the contractor and the owner to undertake the project and is preferably shared between the two parties. However, since the  
30 subject method advantageously provides a method for risk-sharing between the contractor and the owner, it is preferred that any negative savings (i.e., financial losses) are shared between the contractor and the owner.

0 The sharing of savings between the owner and the contractor can start as soon as savings resulting from the modification can be identified. The savings can be shared between the owner and the contractor in any way they mutually decide. In some cases, it is preferred that the party who paid the costs of implementing the  
5 modification recover from the savings derived from the modification an amount equal to repayment of its costs; then the remainder of the savings are shared between the  
owner and the contractor on the basis of a predetermined proportion that preferably is  
defined in the performance-based contract.

10 One method for sharing this value is to share between the participating parties on an equal basis for a negotiated period of time. Another method for sharing is where a negotiated portion of the excess of the value of the change in the  
productivity-related parameter caused by the modification over the cost of the  
15 modification is shared between the participating parties. In any case, it is preferred that the party bearing the cost for the modification recover such cost prior to any sharing of savings.

20 In some cases, implementation of a modification to the process includes the purchase and installation of capital equipment. By "capital equipment", what is meant is equipment which the Internal Revenue Service would require to be capitalized. This includes most larger or more expensive pieces of equipment and/or equipment having a useful life of over one year. When capital equipment is purchased, the purchaser is normally required to show the equipment on its balance sheet. Thus, if the process owner purchases capital equipment, the cost is normally shown on its balance sheets. However, if the contractor purchases any capital equipment that is required for the modification, the cost appears on the contractor's balance sheet rather than on the balance sheets of the process owner. This is advantageous because it permits the process owner to obtain and take advantage of the new capital equipment without the burden of the purchase on its balance sheet -- thus, freeing its own capital for other projects and increasing overall return on assets.

25 Using statistical productivity improvement models as management tools

30 Many industrial plants have extensive information gathering systems that report data for their processes. Some of this data is reported for productivity-related parameters, such as energy use, consumables use, labor use, production rate, and the

like. However, what is lacking is an accurate standard against which to compare productivity. Often what is used is an accounting standard, such as an average of past performance. However, such a standard does not take into account changes in production levels, product mix, weather conditions, operation of different pieces of

5 equipment in the process, and the like -- all of which can affect productivity.

Compared to this standard, measured productivity can be either positive or negative, but the standard provides no basis for determining whether the measured productivity is good or bad. Such a situation puts management in the position of solving non-existent problems, or ignoring real performance deterioration.

10 It has been found that the statistical productivity models of the present invention can be used in a surprising way to serve as a basis for a reliable decision support system for improved management of process productivity. The productivity model, or models, can be applied to the measured values of the independent variables -- as soon as they are available -- to provide an almost instantaneous comparison of 15 the process productivity with the productivity that would have been expected without present improvements or modifications to the process. In other words, the model indicates whether process productivity is actually improving or degenerating.

The general procedure for using the models as management tools is shown in Figure 1. Following approval of the proposed modification(s) by the owner, the 20 contractor and the owner use the model(s) to monitor the improvement(s) due to the implemented modifications to the process. This monitoring is performed by using models that cover the total industrial process, or even more than one process, if present in the industrial plant, and also by using the models for each of the unit processes. Data for each dependent variable and each independent variable in the 25 validated set is collected and preferably segregated into months. From these monthly data sets, monthly reports can be generated. The monthly reports indicate -- for each day of the month -- the cumulative savings resulting from the implemented modifications, and also, in the case of a monthly plant-wide report, serve as the basis for sharing the resulting cost savings by which the contractor is paid (as described 30 above).

The application of certain control rules to the daily data, as defined below, indicate when monitored data reveals processes to be outside statistical control, at which point various remedial measures, as indicated in Figure 1, can be quickly taken.

One specific way that the models are used as a management tool is to plot the 5 productivity-related parameter versus time in the form of a daily report. If the value of the productivity-related parameter predicted from each day's values of the independent variables is also plotted on the same chart, or otherwise compared against the actual value of the parameter, the positive or negative deviation from the predicted value can be readily envisioned. Moreover, if data from several weeks or months is 10 included in the chart, any trends in the productivity can also be seen. This can be seen in Figure 3, where daily energy use is plotted versus time along with the predicted value of energy use and the value of the energy savings. The plot provides a clear indication of what actual energy use was for the previous 24 hours and what it should have been -- given the operating conditions, production rates and weather conditions 15 that prevailed. The application of simple statistical control tools to plots such as this, as will be discussed in more detail below, can provide an accurate means of determining when to make a process change or when to analyze the process further to solve a problem or take advantage of an opportunity.

One preferred method for the analysis of data of the type illustrated in Figure 4 20 is analysis according to tests such as, for example, those sometimes known as the "Western Electric Zone Tests". (See, e.g. *Understanding Statistical Process Control*, by Donald Wheeler and David Chambers, SPC Press (1992), for more information). One embodiment of the application of these tests to the data of Figure 4 is to examine the difference between each day's value of the productivity-related parameter and the 25 predicted value of that parameter according to four rules. If any point results in a violation of one of these rules, then the process must be investigated to determine what special cause of variability has occurred to bring the process out of statistical control. The rules are as follows:

30 Rule 1: Any point more than three standard deviations from the process average;  
Rule 2: Any two out of three successive points on the same side of, and more than two standard deviations from, the process average;

Rule 3: Any four out of five successive points on the same side of, and more than one standard deviation from, the process average; or

Rule 4: Any eight successive points on the same side of the process average.

5        It is believed that if any one of these patterns of productivity variability occurs, it is an indication that there is a special cause of variability that is not accounted for by the productivity model. Usually these special cases result in deterioration of the productivity of the process, but occasionally a change occurs that results in improvement. In any case, it is important to identify either productivity  
10      deterioration or improvement for the process to support timely correction or making a transient improvement permanent.

The same tests as listed above can also be used to determine the effect of a planned and consciously implemented change to the process as a part of a test. If the change does not result in a rule violation, then the change did not affect the process.

15       Once the industrial process of interest has achieved a new, more efficient, level of productivity through application of the present method, it is preferred that a new mathematical model is constructed and the entire subject method is repeated. The new model then becomes the standard for determining the performance of the improved process.

20       The following examples describe preferred embodiments of the invention. Other embodiments within the scope of the claims herein will be apparent to one skilled in the art from consideration of the specification or practice of the invention as disclosed herein. It is intended that the specification, together with the examples, be considered exemplary only, with the scope and spirit of the invention being indicated  
25      by the claims which follow the examples.

#### EXAMPLE 1

30       This is an example of a performance-based contract for an energy-savings modification that could be used in one embodiment of the present invention. It is intended that any blanks that appear would be filled in by inserting information appropriate to the particular parties, time and terms and conditions.

ENERGY COST SAVINGS AGREEMENT

BETWEEN

5

OWNER  
and

CONTRACTOR

THIS AGREEMENT made and dated this \_\_\_\_\_ day of \_\_\_\_\_, \_\_\_\_\_ by and  
between OWNER ("CLIENT") and CONTRACTOR, a \_\_\_\_\_ Corporation.  
10 WHEREAS, CONTRACTOR is engaged in the business of developing and  
implementing energy cost savings plans including (i) the design and implementation  
of energy management systems; (ii) the development and installation of energy  
related instruments, equipment, and devices for which CONTRACTOR shall provide  
all funding through itself or a funding source (the "Funding Source"); (iii) and, at the  
15 option of CLIENT, other capital projects which enhance energy savings, productivity,  
and other benefits ("Capital Projects");

WHEREAS, CLIENT desires to engage CONTRACTOR to perform certain  
services in connection with the operations at CLIENT's Facility which facility is  
located \_\_\_\_\_. (the "Facility");

20 NOW, THEREFORE, for good and valuable consideration, the receipt and  
sufficiency of which are hereby acknowledged, the parties hereto agree as follows:

Section 1: Engagement of CONTRACTOR and Energy Savings PlanDesign

25 CLIENT hereby engages CONTRACTOR to design for implementation a plan  
of cost savings (the "Plan") with respect to energy consumption and general  
operations at the Facility. Cost savings ("Cost Savings") shall be calculated and  
determined based upon Statistical Mathematical Models ("Models") to be developed  
by CONTRACTOR, and approved by CLIENT. Such Cost Savings will be calculated  
0 by subtracting the actual energy usage during each monthly billing period from the  
30 baseline usage ("Baseline Usage") predicted by the Models. A separate Model will be  
constructed for each significant energy-using process in the plant ("Plant Wide  
Models"). After acceptance of the Model(s) by CLIENT if any changes are made at  
the Facility or to the production process which substantially affect variables related to

energy consumption, then, in that event the Models shall be adjusted to reflect those changes.

Section 2: Definition of Time Periods During Agreement

This agreement shall commence on \_\_\_\_\_ (the "Commencement Date"). CONTRACTOR shall complete and submit the Plan for CLIENT approval by \_\_\_\_\_ but in no event later than 90 days after the Commencement Date. This 90 day period from the Commencement Date to the submission of the plan shall be referred to as the "Analysis Period". The 90 day period immediately following the Analysis Period, from \_\_\_\_\_ through \_\_\_\_\_ shall 5  
10 be referred to as the "Implementation Period". During the Implementation Period CLIENT and CONTRACTOR shall jointly begin implementation of the Plan based solely upon approval of specific improvements by CLIENT, which approval shall not be unreasonably withheld or denied. Measurement of Cost Savings pursuant to this Agreement shall commence on \_\_\_\_\_, and terminate on the date twenty- 15  
15 four (24) full months, following on \_\_\_\_\_. This 24 month period of time 0  
0 shall be known as the "Shared Savings Period". It is understood by both parties that implementation of the Plan, and additions to the Plan which CONTRACTOR shall make from time-to-time, will continue after the end of the Implementation Period, but fees paid to CONTRACTOR from any implementation of any part of the Plan will 20  
20 end on \_\_\_\_\_. CONTRACTOR shall provide written notice to CLIENT of the Commencement Date, the end of the Analysis Period, the end of the Implementation Period and the beginning of the Shared Savings Period. In the event that cessation of all or part of operations at the Facility (of more than two weeks in length during the term of contract) occur, then in that event, the Shared Savings 25  
25 Period shall be extended for a period(s) of time beyond \_\_\_\_\_ with such extension(s) to be mutually agreed upon by both parties.

Section 3. Implementation of Plan

Upon approval of the Plan and the Model(s) by CLIENT, which approval shall not be unreasonably withheld or delayed, CLIENT and CONTRACTOR shall during 30 the entire term of this Agreement, jointly implement the recommendations of CONTRACTOR embodied in the Plan, provided such recommendations shall not, following implementation, impair operations or productions or create unsafe working

conditions at the Facility. CLIENT shall provide such personnel as CONTRACTOR may direct, including, without limitation, administrative, operations and maintenance personnel for the purpose of implementing those recommendations which relate to routine administrative, operations and maintenance procedures, including deferred maintenance; provided that the use of such personnel by CONTRACTOR shall not unreasonably impair CLIENT's usual operations. CONTRACTOR shall bear the direct costs of specialty equipment, expert personnel, specialized consultants, and other costs not incurred in the ordinary course of maintenance and operation of the Facility required to implement Plan recommendations, other than improvements requiring Capital Projects discussed in the Section immediately below.

#### Section 4. Capital Projects Recommendation

Capital Projects identified by CONTRACTOR during development and implementation of the energy management system relating to energy and/or production cost improvements will be submitted as a separate financial proposal from this agreement. CLIENT shall not be obligated to agree to make any such Capital Projects that CONTRACTOR recommends.

#### Section 5. Fee Structure and Conditions

In consideration of the services rendered by CONTRACTOR under this agreement, CLIENT shall pay CONTRACTOR a fee (the "Fee") equal to fifty percent (50%) of all cost reductions resulting from the Plan and realized by CLIENT during the Shared Savings Period. Energy and related costs reductions include but are not limited to reduction in the use and or cost of electricity, natural gas and other fossil fuels, electrodes, oxygen, nitrogen, argon, carbon, refractories, water, steam and productivity improvements. During the term of the Shared Savings Period, Cost Savings shall be those measured by the Model. The recording instruments and calibration methodologies providing data for the Model shall be mutually agreed upon by both parties.

#### Section 6. Terms of Payment

Each month for the 24 month period beginning \_\_\_\_\_ and 30 ending \_\_\_\_\_, (the Shared Savings Period) the fees described in paragraph 5 will be paid as follows: During the Shared Savings Period, CONTRACTOR will bill CLIENT by the 15<sup>th</sup> day of each month, the amount of

energy savings for the immediate preceding month as determined by the Models. Such invoices as well as any payments for capitalized equipment under Section 18 0 | hereinafter will be payable net 10 days and shall be paid to a lockbox of the Funding | Source as Identified in Exhibit \_\_\_\_ attached hereto and incorporated herein by this 5 | reference, provided that such address for payment may only be changed from time to | time by the Funding Source by written notice to CLIENT and CONTRACTOR (it | being understood that the provisions of this sentence are for the express benefit of the | Funding Source). For the duration of the contract term CLIENT shall provide | CONTRACTOR with accurate and adequate energy billing information in a timely | 10 way so as to allow CONTRACTOR to produce accurate and timely invoices.

#### Section 7. Provision of Information and Access to Facilities

Upon commencement of the Analysis Period of this contract, CLIENT shall promptly provide CONTRACTOR with such records and information as CONTRACTOR shall require, including, without limitation, records and information 15 | relating to energy usage, production and quality control, and CLIENT shall furnish | 0 | CONTRACTOR with such space and access to facilities as CONTRACTOR shall reasonably direct. Both parties agree that CONTRACTOR shall have access to such | information on a daily basis. CLIENT shall make records and facilities available to | CONTRACTOR personnel for the term of the contract to enable CONTRACTOR to | 20 | monitor and maintain energy savings. In addition, CLIENT agrees to provide access | to the Facility to the Funding Source during normal business hours upon reasonable | written notice to inspect the energy management systems installed at the Facility |

#### Section 8. Independent Contractor Status

CONTRACTOR is and shall be an independent contractor in the performance 25 | of all services contemplated hereunder. CONTRACTOR shall exercise its own | discretion on the method, manner and performance of such services. The employees, | subcontractors, methods, and equipment used by CONTRACTOR shall at all times be | under its exclusive direction and control. Nothing in this Agreement shall be | construed to designate CONTRACTOR its employees, subcontractors, agents or | 30 | assigns as the employees, subcontractors, agents or assigns of CLIENT.

### Section 9. Confidentiality Requirements

CONTRACTOR shall maintain as confidential and not disclose to others, without CLIENT's prior written consent, all information obtained from CLIENT that is not publicly available. The provisions of this paragraph shall not apply to 5 information in whatever form which (i) is published or comes into the public domain through no fault of CONTRACTOR, (ii) is furnished by or obtained from a third party who is under no obligation to keep the information confidential, or (iii) is required to be disclosed by law or order of a court, administration agency or other authority with proper jurisdiction. CLIENT shall agree to hold confidential all of the operating 10 methods and procedures of CONTRACTOR and shall agree not to divulge such information to any third party or to implement such procedures in CLIENT's other plants or facilities.

### Section 10. Insurance Requirements

CONTRACTOR shall maintain during the term of the Agreement, worker's 15 compensation, and general liability insurance.

### Section 11. Indemnity

CONTRACTOR agrees to defend, indemnify and hold CLIENT harmless from and against any and all claims for loss or damage arising out of the gross negligence of CONTRACTOR with respect to the performance of services hereunder.

### 20 Section 12. Service Modifications

All electrical, steam, air, gas, and other service or equipment shut-offs, start-ups, disconnections, or interruptions (collectively referred to herein as "Service Modifications") shall be performed by authorized personnel of CLIENT. CONTRACTOR shall provide CLIENT with reasonable prior notice of all Service 25 Modifications for CLIENT's approval.

### Section 13. Early Termination Provisions

Notwithstanding anything contained herein to the contrary, CONTRACTOR may, at its option, upon the provision of five days written notice to CLIENT, terminate this Agreement without cause at any time on or before \_\_\_\_\_ 30 (the end of the Analysis Period) whereupon neither party shall have any further liability hereunder or obligation to the other party. CLIENT shall have the option to terminate this contract at any time on or before \_\_\_\_\_ (the end of the Analysis

Period), upon five day written notice to CONTRACTOR. Upon early termination by CLIENT, CLIENT shall reimburse CONTRACTOR for all project expenses, including but not limited to CONTRACTOR personnel and consultant costs, directly associated with the services provided by CONTRACTOR to CLIENT. These 5 expenses shall be documented and submitted to CLIENT within five days after CONTRACTOR's receipt of CLIENT's termination notice and paid by CLIENT within five days thereafter. Upon receipt of payment by CONTRACTOR neither party shall have any further obligations to the other and CONTRACTOR shall waive any and all claims under this Agreement. In the event of an early termination, all 10 information developed by CONTRACTOR shall remain the property of CONTRACTOR, and both parties shall continue to be bound by the confidentiality condition of this Agreement.

Section 14. Binding Agreement

This Agreement shall be binding on and shall inure to the benefit of the parties 15 named herein and to their respective successors and assigns.

Section 15. Choice of Law

This Agreement is deemed to be made under and shall be construed according to the laws of the State of \_\_\_\_\_ without regard to its conflicts of law provisions.

20 Section 16. Entire Agreement

This Agreement constitutes the entire agreement between the parties hereto and supersedes all prior agreements, whether oral or written, with respect to the subject matter hereof. No Changes or Amendment to this Agreement shall be binding on either party unless reduced to writing and signed by the parties sought to be bound 25 and consented to by CONTRACTOR's Funding Source.

Section 17. Assignment

CONTRACTOR shall not assign this Agreement without the prior written consent of CLIENT, provided that CLIENT consents to the assignment of this agreement to CONTRACTOR's Funding Source and agrees that the Funding source 30 may succeed to CONTRACTOR's rights hereunder in the event CONTRACTOR is in default hereunder. Further, CLIENT agrees that should CONTRACTOR fail to perform its duties to earn such fees, CLIENT shall inform CONTRACTOR and

CONTRACTOR's Funding Source in writing and shall permit CONTRACTOR to correct or remedy within 30 days. If CONTRACTOR fails to cure such default, CLIENT shall notify CONTRACTOR's Funding Source of such failure and shall permit CONTRACTOR's Funding Source to correct or remedy such default within 30 days, provided, however, that any steps which the Funding Source undertakes to cure or remedy such default on the part of CONTRACTOR, shall be subject to CLIENT's written consent which will not be unreasonably withheld. CLIENT shall not assign this Agreement without the prior written consent of CONTRACTOR.

Section 18. Ownership of Equipment

CONTRACTOR shall have the right, and with the consent of CLIENT, to install energy related instruments, equipment, and devices ("Equipment") with which to accomplish its energy cost reduction goals as contemplated in this Agreement. During the term of this Agreement the title to all such Equipment shall remain with CONTRACTOR. To the extent any of the Equipment is capitalized by CONTRACTOR in accordance with Generally Accepted Accounting Principles, then, at the end of the Shared Savings Period, CLIENT shall have the option of purchasing such capitalized Equipment at its fair market value as agreed to by the parties or CONTRACTOR may abandon such Equipment. In any event, CONTRACTOR shall have no obligation to remove such Equipment from the Facility and CLIENT agrees to assume ownership and title to all such Equipment upon final payment due to CONTRACTOR, or its assign, under the terms of this Agreement. In the event CLIENT elects to purchase the capitalized Equipment from CONTRACTOR, CONTRACTOR will provide CLIENT with a Bill of Sale for such equipment within 30 days after the end of the Shared Savings Period. Notwithstanding the aforesaid, in the event CLIENT elects to purchase the capitalized Equipment from CONTRACTOR, the purchase price thereof shall be calculated and included as part of the final fee payment(s) due to CONTRACTOR hereunder unless otherwise agreed to by the parties.

Section 19. Warranties

CONTRACTOR makes no representations or warranties concerning the services to be performed hereunder, including, without limitation, the amount of Cost

Savings to be realized by CLIENT following implementation of the Plan and recommendations of CONTRACTOR.

Section 20. Notices

Any notice or other communication in connection with this Agreement shall

5 be in writing, addressed as provided below and (i) deposited in the United States Mail, postage prepaid, by registered or certified mail, or (ii) hand delivered by any commercially recognized courier service or overnight delivery service such as Federal Express, addressed:

IN WITNESS WHEREOF, the parties hereto have caused this Agreement

10 dated \_\_\_\_\_ containing \_\_\_\_\_ pages to be executed as of the date written below.

CONTRACTOR

CLIENT

By: \_\_\_\_\_

By: \_\_\_\_\_

Name: \_\_\_\_\_

Name: \_\_\_\_\_

15 Title: \_\_\_\_\_

Title: \_\_\_\_\_

Date: \_\_\_\_\_

EXAMPLE 2

This illustrates the derivation of a statistical mathematical model of the natural  
20 gas consumption in a forging operation in the Midwestern United States.

The model equation for natural gas consumption for an industrial forging operation in the upper Midwestern United States was obtained by applying the following procedures:

Historical values of gas consumption for the process were obtained from daily  
25 energy reports for the period April of one year through January of the next year, giving a total of 304 data points. Production and weather data for the same period was gathered from daily production reports and from Midwest Climate Center reports for Chicago's Midway Airport, respectively.

A multiple regression analysis (using the multiple linear regression routine  
30 provided by Lotus<sup>TM</sup> 1-2-3, release 5) for the following independent variables:

Production (Pounds)

Heating degree days (HDD)

Production work days (PWD)

Office work days (OWD)

This analysis gave an equation of the form:

5       $E_T = 2119 + 0.0287 * (\text{Pounds}) + 177.8 * (\text{HDD}) + 9473 * (\text{PWD}) + 2787 * (\text{OWD})$   
where,

$E_T$  = total natural gas usage.

The R-squared value for this analysis was 0.8154 and the average day-to-day variation was 16.87%. Taken over the monthly periods for this historical data, this 10 gave a month-to-month variation of about 8%, which was considered to be too high for acceptable accuracy (no more than 5% is considered acceptable for monthly variation).

The data was then sorted by day of the week and an attempt was made to see if there were any significant trends. (For example, it was thought that a start-up on 15 Monday after a week-end would show higher gas usage.) This analysis showed that there was a systematic underprediction of gas use on Saturdays when there was no production. Upon questioning the production management, it was found that normally there was a cleaning crew on duty part of the day on Saturday and it was necessary for the boiler to be operated during this time. If Saturday was a production 20 day, this did not make a significant difference, but the gas use was significantly different from Sundays, when the boiler was not operated. As a result of this finding, non-production Saturdays was added as an independent variable. This regression improved the R-square slightly from 0.8154 to 0.8175 and reduced the day-to-day variation to 15.9% -- which was still too high.

25      Another complicating factor in this analysis was the fact that the parts produced in this process varied widely in size, from a few pounds to more than 1,000 lbs. It was decided to sort production by size of part produced. Initially, production was sorted into six groups: up to 25 lbs; 25 - 50 lbs; 50 - 100 lbs; 100 - 200 lbs; 200 - 500 lbs; and more than 500 lbs. A regression analysis using these groupings yielded 30 unstable results with very unreliable coefficients. The number of groupings was reduced gradually until just two groups were used. A finer separation by part size did not improve the correlation. The two groupings that were used were parts larger than

100 lbs, but less than 500 lbs, and parts larger than 500 lbs. It was found that production of parts smaller than 100 lbs (initial size) did not affect gas use. This analysis improved R-square to 0.82, but did not materially affect the day-to-day error.

Throughout the analysis, the months of May and June of the first year were 5 consistently underpredicted, with actual gas use being considerably above the model predictions. Review of the energy reports showed that a different boiler was in use during much of this period. As a result of this, operation of this second boiler was included as an independent variable in the regression analysis. This addition improved the R-square from 0.82 to 0.8452, with a subsequent reduction in day-to-10 day error to 15.4%.

Frequently, the relationship between the measured (dependent variable) and the factors affecting it are non-linear. The technique used to test for linearity is to sort the data -- using each independent variable in turn as a sorting key. The variables amenable to this sorting were daily production quantities and daily heating degree 15 days. No systematic trend in the deviation between the model and the actual gas use was determined for production levels, but a significant difference was found at very high degree days. The practical reason for this is that when it is extremely cold, the boiler is run around the clock to prevent problems with frozen pipes; the normal practice being to shut the boiler down at the end of a production day. As a result, gas 20 use during a very cold day is substantially higher than normal. The systematic deviation was averaged for days greater than 45 degree days and found to be approximately 8,000 therms more than the model prediction.

In order to apply this correction to the model, the daily actual gas use was reduced by 8,000 therms for any day with more than 50 heating degree days, and the 25 regression analysis was rerun using the adjusted actual gas use as the dependent variable. This regression showed an R-square of 0.8703 and an average day-to-day variation of 13.9% -- a considerable improvement.

A model based on regression analysis can be made to fit a set of historic data to almost any degree of accuracy, given enough independent variables. This accuracy 30 does nothing to indicate how good the model is as a predictive tool. To measure the model's usefulness as a predictor, it must be applied to a set of data for the same process, which was not included in the data used to derive the model.

In this case, the model was applied to data from February and March of the second year. February fit quite well -- with the model underpredicting actual use by 5.7%, but March was not a good fit with the model -- overpredicting by 16.5%. When this was discussed with the production management, they recognized that a large

5 piece of process equipment had been shut down on March 2, of the second year for an extensive rebuild. For the present purposes, this piece of equipment will be referred to as a Steam User. Since no data was available specifically for the energy load related to the Steam User, it was decided to calculate the average difference between predicted and actual gas use for the 30 days during March when this piece of  
10 equipment was down. This was calculated at 3026 therms per production day. When this information was added to the model, the final model equation had the form:

$$E_T = 1906 * B + 5944 * PWD + 3026 * SUD + 1900 * NPS + 0.04684 * P1 + 0.02770 * P2 + 2857 * OWD + 163.9 * HDD + 3646 * Z + 8,000$$

where:

15  $E_T$  = Total gas use during the period (Therms);  
B = Number of days in the period;  
PWD = Number of production days in the period;  
SUD = Days of operation of Steam User;  
NPS = Number of non-production Saturdays in the period;  
20 P1 = Production pounds for units of greater than 100 lbs, but less than 500 lbs;  
P2 = Production pounds for units of greater than 500 lbs;  
OWD = Office workdays in the period;  
HDD = Heating degree days in the period;  
Z = Days of operation of second boiler.  
25 8,000 therms was added for any day having HDD 50 or over, but was not added for any day having HDD under 50.

The R-square value for this model is 0.894 and the monthly deviation was less than 5%, both of which are within the accuracy required of the model.

#### EXAMPLE 3.

30 This example illustrates the modification of the control system of a tube mill furnace and the sharing of savings obtained as a result of the modification.

A performance-based contract, similar to that shown in Example 1, was established between the owner of a tube mill and an independent contractor. A statistical mathematical model was derived for the metal tube manufacturing process by the method illustrated in Example 2. As a result of process simulations of a number of potential process modifications, it was found that the productivity of the system could be significantly improved by modifying the gas and air control system of the furnace and thereby saving energy. The system upgrade involved replacing an Askania ratio control system with an electronic system using an existing programmable limit controlled PLC-5/25. The new system was designed to sense combustion air flow on the downstream side of the furnace recuperators, eliminating errors due to recuperator leakage. Gas and air flow measurements were temperature compensated and gas flow measurement was also pressure compensated.

Air flow was measured by a set of two pitot tubes in each zone. Natural gas flow was measured using an orifice plate in at the same location as an existing orifice plate. The flow signals (differential pressures) were sensed locally, eliminating the need for impulse lines leading to the pulpit. All input and output features outside of the pulpit were directed through a remote I/O enclosure located near the steam superheater control box.

The existing natural gas valve actuators and stack damper actuator were used, but gas flow, pressure and temperature sensors, and combustion air flow, temperature and air actuators were new. The existing furnace temperature and pressure sensors and gas actuators were used.

Operator interface was via a flat-panel LCD Panel View 550 unit with keypad entry. The control algorithm provides the option of automatic gas and air flow driven from user-supplied zone temperature inputs, or user-supplied air or gas flow with automatic ratio control. The algorithm also provides cross-limited, cascade control. The system also has the capability of displaying instantaneous energy usage rate (MMBTU/TON) on the Panel View screen for instantaneous feedback of energy use rate to the operators.

**30      Role of the Contractor and the Owner (Client):**

The contractor provided the equipment as listed below in Table 1. The contractor also provided programming and engineering services and engineering

support throughout the installation and implementation of the modification as shown in Table 2.

The installation of the combustion air pitot tubes involved technical support from the manufacturer and labor from the client as shown in Table 3. All other transmitters were mounted and installed by the client. All cables and conduits were installed using client labor. All client labor costs was paid by the contractor.

Table 1: List of new components purchased and installed in the modification.

QUANTITY	ITEM	PRICE	TOTAL PRICE
4	Rosemount 1151 DP, 0 - 25" wc	\$1,159.00	\$4,636.00
3	Rosemount 3051 CD 0 - 0.5" wc	1,598.00	4,794.00
1	Pyromation RTD and Transmitter	613.00	613.00
6	Superior Flo 1005 series pitot tubes	1,260.00	7,560.00
3	Orifice plates (natural gas)	309.00	927.00
3	Tru-Tork MATIC TA400 damper actuators	1,761.00	5,283.00
1	Allen-Bradley 1771-IFE 16 point analog input cards	1,087.00	1,087.00
2	Allen-Bradley 1771 OFE2 4 point output cards	1,087.00	2,174.00
1	Allen-Bradley 1771-IA Mini AC/DC (120V) input card	250.58	250.58
1	Allen-Bradley 1771-OA AC/DC (120V) output card	350.58	350.58
1	Panel View 550 Operator Terminal	1,695.00	1,695.00
1	Configuration software for Panel View	495.00	495.00
1	Allen-Bradley 1771-P4S power supply	460.63	460.63
1	Allen-Bradley 1770-SC Data Highway station	184.25	184.25
1	Allen-Bradley 1771-ASB Remote I/O Adapter	847.55	847.55
1	NEMA-4 30"x24"x10" enclosure	265.00	265.00

.1	30"x24" panel	35.00	35.00
1	Allen-Bradley 1771-A2B 64 I/O Rack Assembly	305.86	305.86
3	Current isolators for single input card cables and conduit	225.00	675.00
<b>TOTAL</b>			<b>\$32,638.69</b>

Table 2: Contractor labor expended during the modification.

FUNCTION	MANHOURS	RATE	TOTAL CHARGE
Programming	200	\$80/manhour	\$16,000.00
Engineering	120	\$80/manhour	3,600.00
Installation support	120	\$60/manhour	3,600.00
<b>TOTAL</b>			<b>\$23,200.00</b>

Table 3: Client labor expended during the modification.

FUNCTION	MANHOURS	RATE	TOTAL CHARGE
Electrician	708	\$42.60/manhour	\$32,035.00
Pipefitters	130	\$42.60/manhour	5,538.00
Instrument repair	80	\$42.60/manhour	3,408.00
<b>TOTAL</b>			<b>\$40,981.00</b>

5

Results:

The tube mill furnace controls project was commenced in March of the project year and completed in May of that same year, with full operation achieved in June. Fuel use, which had averaged more than 45,000 MMBTU per month, was reduced to 10 an average of slightly more than 32,000 MMBTU per month. The actual gas usage rates before and after the implementation of the modification are shown in Figure 5, along with the gas usage rate predicted by the mathematical model for the system had the modification not taken place (the predicted rate). Average natural gas cost over the shared savings period was \$2.71/MMBTU and the savings were shared equally 15 between the client and the contractor. The total investment for this project was approximately \$122,000 -- all of which was paid by the contractor. Total contractor

billings to the client over the shared savings period were about \$425,000. During the contract period, this project provided the client with a net benefit of \$425,000 and the contractor with a net benefit of \$303,000.

All references cited in this specification (including without limitation all 5 citations to journals, periodicals, texts, manuscripts, patents, published patent applications, and the like) are hereby incorporated by reference. The discussion of references herein is intended merely to summarize the assertions made by their authors and no admission is made that any reference constitutes prior art. Applicants reserve the right to challenge the accuracy and pertinency of the cited references.

10 In view of the above, it will be seen that the several advantages of the invention are achieved and other advantageous results obtained.

As various changes could be made in the above methods and compositions without departing from the scope of the invention, it is intended that all matter contained in the above description and shown in the accompanying drawings shall be 15 interpreted as illustrative and not in a limiting sense.

What is claimed is:

1. A method for obtaining savings in an industrial process having an owner comprising establishing a performance-based contract between the owner and a contractor; deriving with a computer a statistical mathematical model that describes a productivity-related parameter for the industrial process in terms of independent variables; identifying a modification that will improve the productivity-related parameter; and implementing the modification.
2. The method as set forth in claim 1 wherein the performance-based contract further provides that the contractor will finance at least part of and will implement the modification that will improve the productivity-related parameter; and that the owner will share the savings that result from the improvement with the contractor.
3. The method as set forth in claim 2 wherein the performance-based contract further provides that the owner and the contractor agree on the model prior to the implementation of the modification.
4. The method as set forth in claim 3 wherein the performance-based contract further provides that the contractor has sufficient authority to manage the implementation of the modification.
5. The method as set forth in claim 2 wherein the independent variables of the statistical mathematical model form a validated set of independent variables.
6. The method as set forth in claim 5 further comprising measuring the savings caused by the modification by determining the difference between a measured value of the parameter and a value of the parameter predicted by the model using measured values of each of the independent variables of the validated set.
7. The method as set forth in claim 6, where the industrial process includes process equipment having a size and in which an amount of capital is invested, and which process uses consumables, energy and labor for the production of one or more products; wherein the productivity-related parameter is production per unit of time, production per unit of labor, production per unit of energy use, production per unit of consumables use, production per unit of process equipment size, production per unit of capital invested in the process, energy use per unit time, consumables use per unit time, or the inverse of any of these.

8. The method as set forth in claim 7, wherein the modification to improve the productivity of the process is carried out without affecting an independent variable that is included in the validated set.

9. The method as set forth in claim 8, wherein the productivity-related parameter is energy use per unit time.

10. A method as set forth in claim 9, wherein the step of deriving with a computer a statistical mathematical model that describes a productivity-related parameter for the industrial process in terms of a validated set of independent variables comprises deriving with a computer a model of production per unit of process energy use having the form:

$$E_T = r_B + \sum_{k=1}^n E_k$$

where:

10  $E_T$  is the energy use for the total industrial process per unit time;

$r_B$  is a constant representing the base energy load for the total industrial process per unit time;

$n$  is the total number of unit processes in the industrial process;

15  $k$  is the identifying numeral for one of the  $n$  unit processes and is a positive integer from 1 to  $n$ ; and

$E_k$  is the energy use for the  $k^{\text{th}}$  unit process per unit time.

11. A method as set forth in claim 10, wherein  $E_k$  is derived for each of the unit processes from a formula having the form:

$$E_k = r_{Bk} + \sum_{j=1}^i r_{kj}(V_j)^m$$

where:

$E_k$  is the energy use for the  $k^{\text{th}}$  unit process per unit time;

$r_{Bk}$  is a constant representing the base energy load for the  $k^{\text{th}}$  unit process per unit time;

10  $V_j$  is the  $j^{\text{th}}$  significant independent variable for the  $k^{\text{th}}$  unit process;

$r_{kj}$  is the linear regression coefficient for the  $j^{\text{th}}$  independent variable in the  $k^{\text{th}}$  unit process that provides the best fit in a correlation of the effects of  $V_j$  upon  $E_k$  as determined by multiple regression analysis of historical data;

15      $m$  is a best fit constant correlating the effect of  $V_j$  upon  $E_k$  as determined by multiple regression analysis of historical data and is a fraction or whole number from 0 to about 3;

$j$  is a number designating one of the significant independent variables in the  $k^{\text{th}}$  unit process and is an integer from 1 to  $i$ ; and

20      $i$  is that number of significant independent variables in the  $k^{\text{th}}$  unit process that comprise a set of significant independent variables for that process.

12. The method as set forth in claim 8, wherein the productivity-related parameter is production of products per unit time.

13. The method as set forth in claim 12, wherein the step of deriving with a computer a statistical mathematical model that describes a productivity-related parameter for the industrial process in terms of a validated set of independent variables comprises deriving with a computer a model of production per unit of time having the form:

$$P_T = s_B + \sum_{k=1}^n P_k$$

where:

10      $P_T$  is the production for the total industrial process per unit time;

$s_B$  is a constant representing the base production for the total industrial process per unit time;

$n$  is the total number of unit processes in the industrial process;

15      $k$  is the identifying numeral for one of the  $n$  unit processes and is a positive integer from 1 to  $n$ ; and

$P_k$  is the production for the  $k^{\text{th}}$  unit process per unit time.

9. A method as set forth in claim 8, wherein  $P_k$  is derived for each of the unit processes from a formula having the form:

$$P_k = s_{Bk} + \sum_{j=1}^i s_{kj}(U_j)^m$$

where:

$P_k$  is the production for the  $k^{\text{th}}$  unit process per unit time;

$s_{Bk}$  is a constant representing the base production for the  $k^{\text{th}}$  unit process per unit time;

10  $U_j$  is the  $j^{\text{th}}$  significant independent variable for the  $k^{\text{th}}$  unit process;

$s_{kj}$  is the multiple regression coefficient for the  $j^{\text{th}}$  independent variable in the  $k^{\text{th}}$  unit process that provides the best fit in a correlation of the effects of  $U_j$  upon  $P_k$  as determined by multiple regression analysis of historical data;

$m$  is a best fit constant correlating the effect of  $U_j$  upon  $P_k$  as determined by

15 multiple regression analysis of historical data and is a fraction or whole number from 0 to about 3;

$j$  is a number designating one of the significant independent variables in the  $k^{\text{th}}$  unit process and is an integer from 1 to  $i$ ; and

20  $i$  is that number of significant independent variables in the  $k^{\text{th}}$  unit process that comprise a set of significant independent variables for that process.

14. The method as set forth in claim 8, wherein the productivity-related parameter is consumables use per unit time.

15. The method as set forth in claim 14, wherein the step of deriving with a computer a statistical mathematical model that describes a productivity-related parameter for the industrial process in terms of a validated set of independent variables comprises deriving with a computer a model of consumables use per unit of time having the form:

$$C_T = t_B + \sum_{k=1}^n C_k$$

where:

10  $C_T$  is the consumables use for the total industrial process per unit time;

$t_B$  is a constant representing the base consumables use for the total industrial process per unit time;

$n$  is the total number of unit processes in the industrial process;

15  $k$  is the identifying numeral for one of the  $n$  unit processes and is a positive integer from 1 to  $n$ ; and

$C_k$  is the consumables use for the  $k^{\text{th}}$  unit process per unit time.

16. The method as set forth in claim 15, wherein  $C_k$  is derived for each of the unit processes from a formula having the form

$$C_k = t_{Bk} + \sum_{j=1}^i t_{kj}(W_j)^m$$

where:

$C_k$  is the consumables use for the  $k^{\text{th}}$  unit process per unit time;

$t_{Bk}$  is a constant representing the base consumables load for the  $k^{\text{th}}$  unit process per unit of time;

10  $W_j$  is the  $j^{\text{th}}$  significant independent variable for the  $k^{\text{th}}$  unit process;

$t_{kj}$  is the multiple regression coefficient for the  $j^{\text{th}}$  independent variable in the  $k^{\text{th}}$  unit process that provides the best fit in a correlation of the effects of  $W_j$  upon  $C_k$  as determined by multiple regression analysis of historical data;

$m$  is a best fit constant correlating the effect of  $W_j$  upon  $C_k$  as determined by

15 multiple regression analysis of historical data and is a fraction or whole number from 0 to about 3;

$j$  is a number designating one of the significant independent variables in the  $k^{\text{th}}$  unit process and is an integer from 1 to  $i$ ; and

20  $i$  is that number of significant independent variables in the  $k^{\text{th}}$  unit process that comprise a set of significant independent variables for that process.

17. The method as set forth in claim 8, wherein a set of historical operating data has been collected for values of the productivity-related parameter and for values of one or more independent variables and such set of historical data is divided into a correlation portion and a validation portion; and the statistical mathematical model is

5 derived by using the correlation portion; and wherein a validated set of independent variables is selected as that set of independent variables that provides a statistical mathematical model having a monthly deviation of no larger than  $\pm 5\%$  when tested against the data in the validation portion.

18. The method as set forth in claim 17, wherein the validated set of independent variables is selected as that set of independent variables that provides a statistical mathematical model having a yearly deviation of no larger than  $\pm 1\%$  when tested against the data in the validation portion.

19. The method as set forth in claim 18, wherein the statistical mathematical model has an R-squared value of not under 0.6.
20. The method as set forth in claim 19, wherein the statistical mathematical model has an R-squared value of not under 0.7.
21. The method as set forth in claim 20, wherein the statistical mathematical model has an R-squared value of not under 0.8.
22. The method as set forth in claim 21, wherein the statistical mathematical model has an R-squared value of not under 0.9.
23. The method as set forth in claim 21, wherein the value of  $m = 1$ .
24. The method as set forth in claim 5, wherein the step of identifying a modification to improve the productivity of the process comprises the steps of: using the model to predict productivity changes by simulating the results of one or more proposed modifications of the process; and selecting at least one of the proposed modifications on the basis of the degree to which the predicted productivity changes are an improvement to the process productivity.
25. The method as set forth in claim 24, wherein the step of implementing the modification comprises the purchase and installation of capital equipment.
26. The method as set forth in claim 25, wherein the owner has a balance sheet and the capital equipment is purchased and installed by the contractor.
27. The method as set forth in claim 26, wherein funds for the purchase and installation of the capital equipment are obtained by the contractor from a lender, thereby providing that the debt does not appear on the balance sheet of the owner.
28. The method as set forth in claim 27 wherein the funds are obtained by the contractor from a lender under the terms of a general obligation loan.
29. The method as set forth in claim 28, wherein the general obligation loan is also a non-recourse loan.
30. The method as set forth in claim 24, further comprising the step of calculating the value in terms of money of the change in the productivity-related parameter caused by the modification.
31. The method as set forth in claim 30, wherein the contractor finances at least a substantial part of the cost of the modification.

32. The method as set forth in claim 31, wherein the contractor finances all of the cost of the modification.

33. The method as set forth in claim 32, wherein the savings that result from the modification are shared between the owner and the contractor on an equal basis for a negotiated period of time.

34. The method as set forth in claim 32, wherein a negotiated portion of the savings that result from the modification are shared between the owner and the contractor.

35. The method as set forth in claim 5, further comprising measuring the value of the productivity-related parameter and the independent variables of the validated set on a regular basis; and plotting the measured value of the productivity-related parameter, the value of the productivity-related parameter predicted by the model

5 using the measured values of the independent variables; and the difference therebetween, as a function of time, thereby providing a tool to track and visually present the impact of the modification.

36. The method as set forth in claim 5, further comprising measuring the value of the productivity-related parameter and the independent variables of the validated set on a regular basis; calculating the value of the productivity-related parameter predicted by the model using the measured values of the independent variables; where

5 the difference therebetween is a measure of the impact of the modification upon the productivity-related parameter; and determining whether the process is statistically out of control by testing the impact versus time data against Western Electric Zone Tests.

37. The method as set forth in claim 5, further comprising measuring the value of the productivity-related parameter and the one or more independent variables on a regular basis; and plotting the measured value of the productivity-related parameter, the value of the productivity-related parameter predicted by the model using the

5 measured values of the independent variables of the validated set; and the difference therebetween, as a function of time, thereby providing a tool to help identify any trend of the productivity-related parameter due to the impact of the modification.

1/13

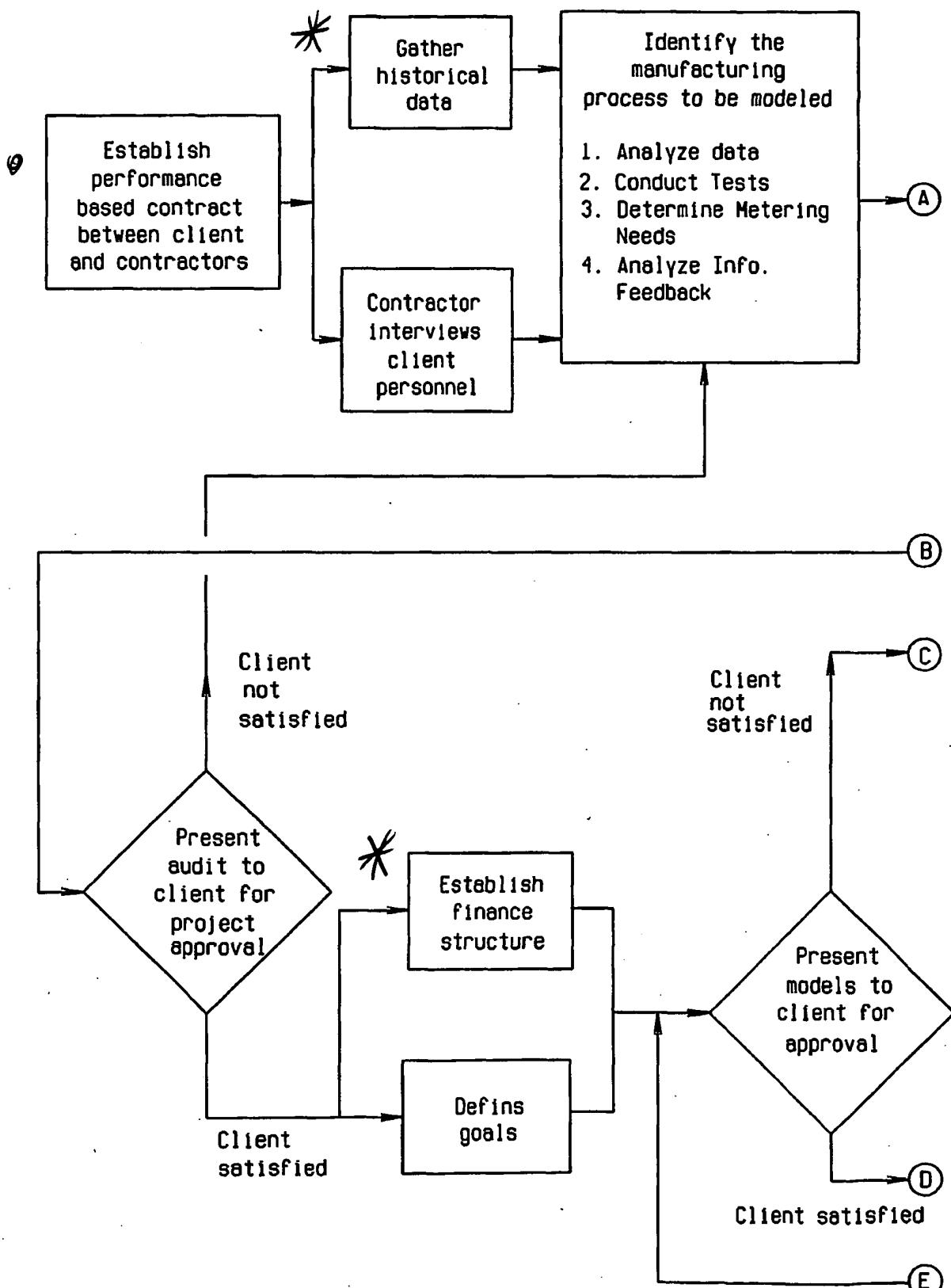


FIG. 1A

2/13

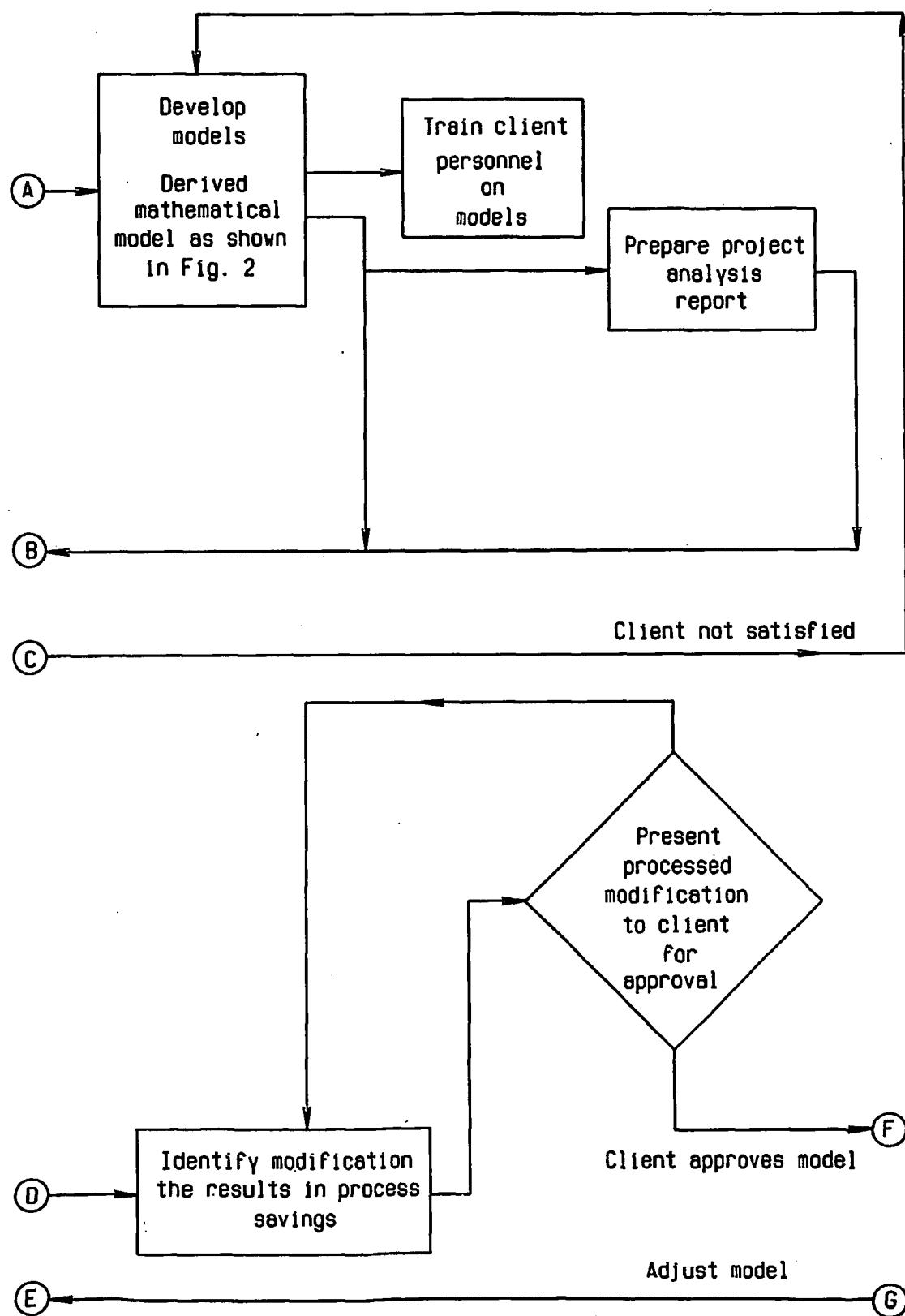


FIG. 1B

3/13

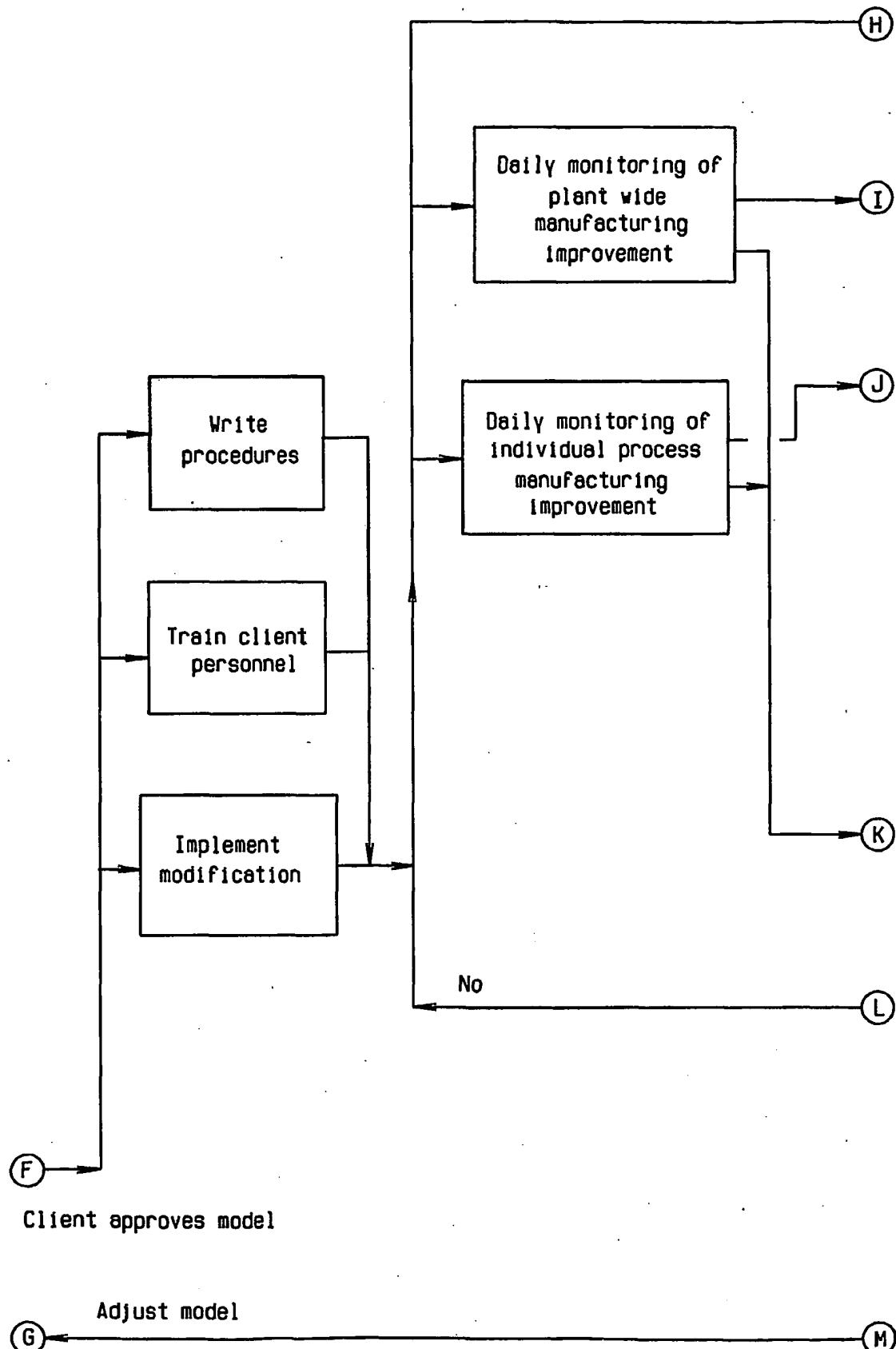


FIG. 1C

4/13

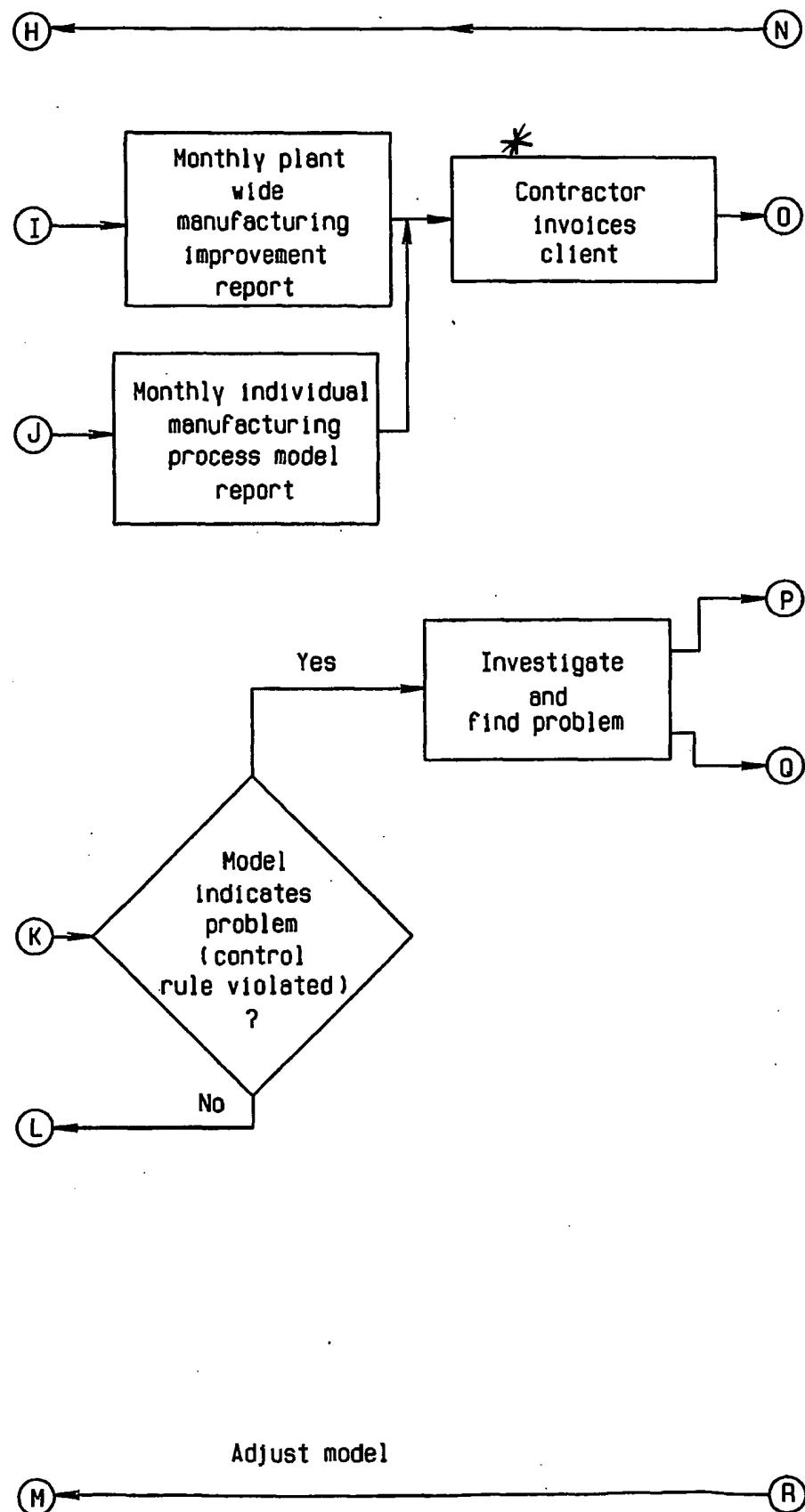


FIG. 1D

5/13

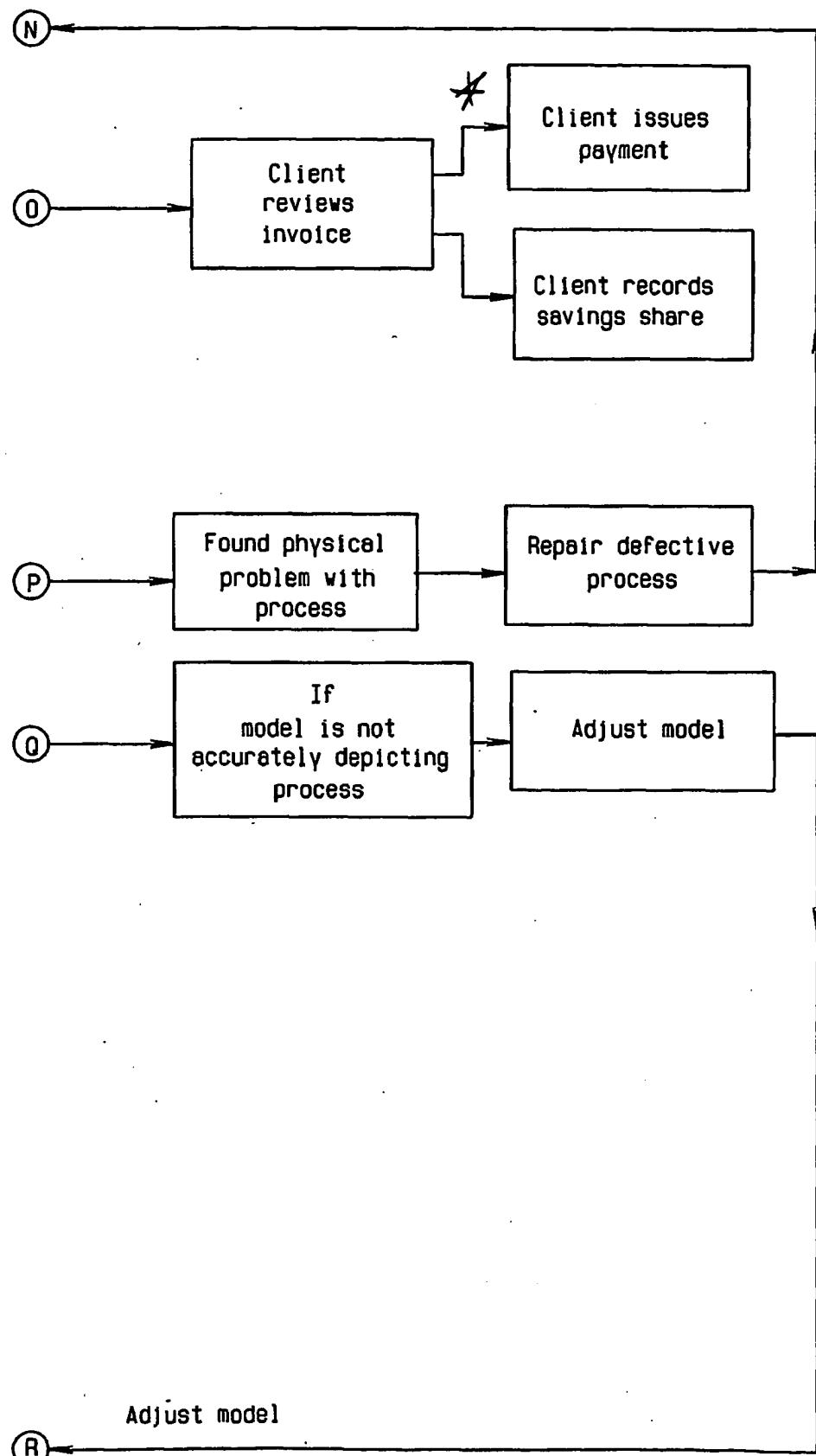


FIG. 1E

6/13

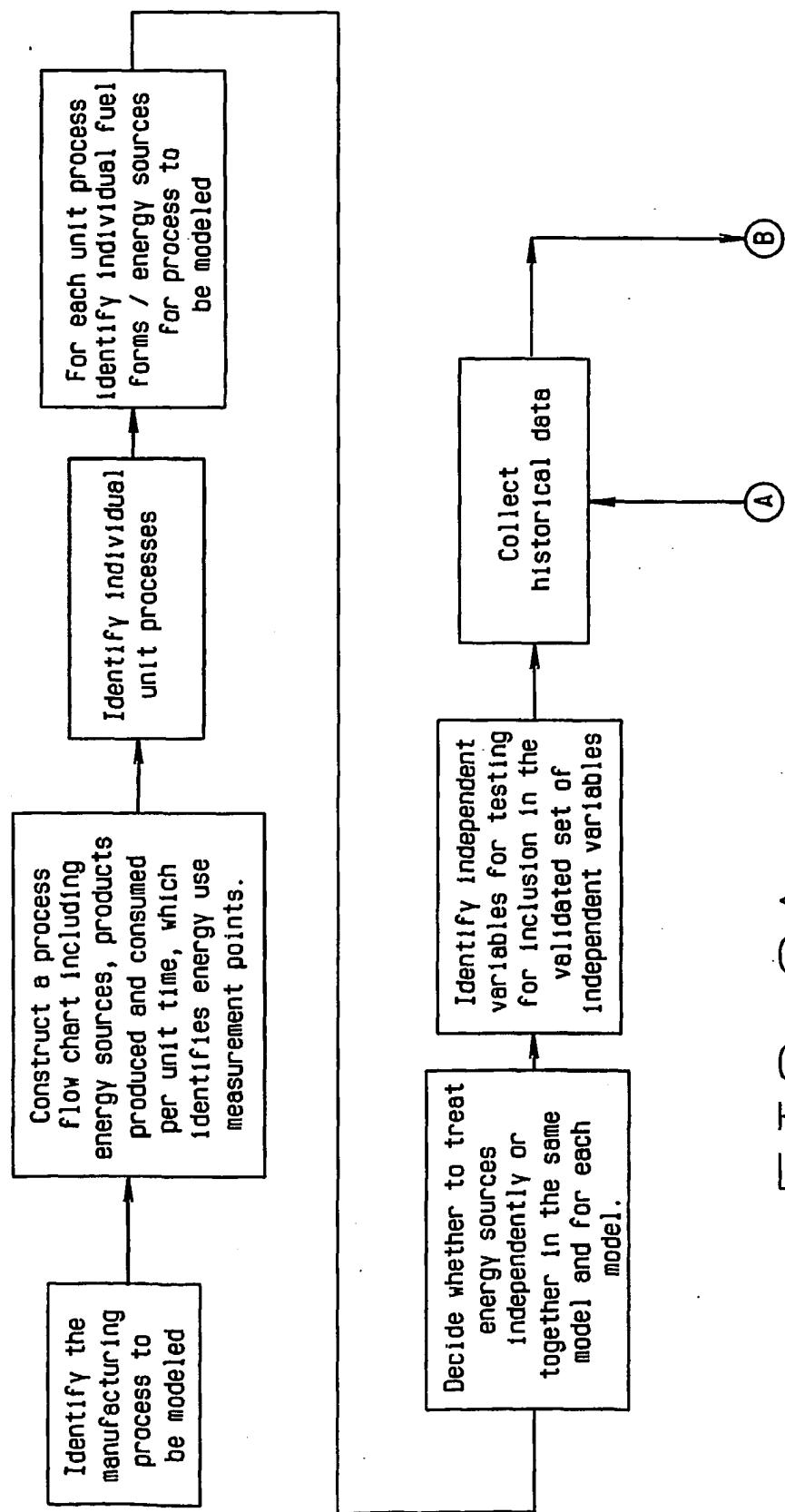


FIG. 2A

7/13

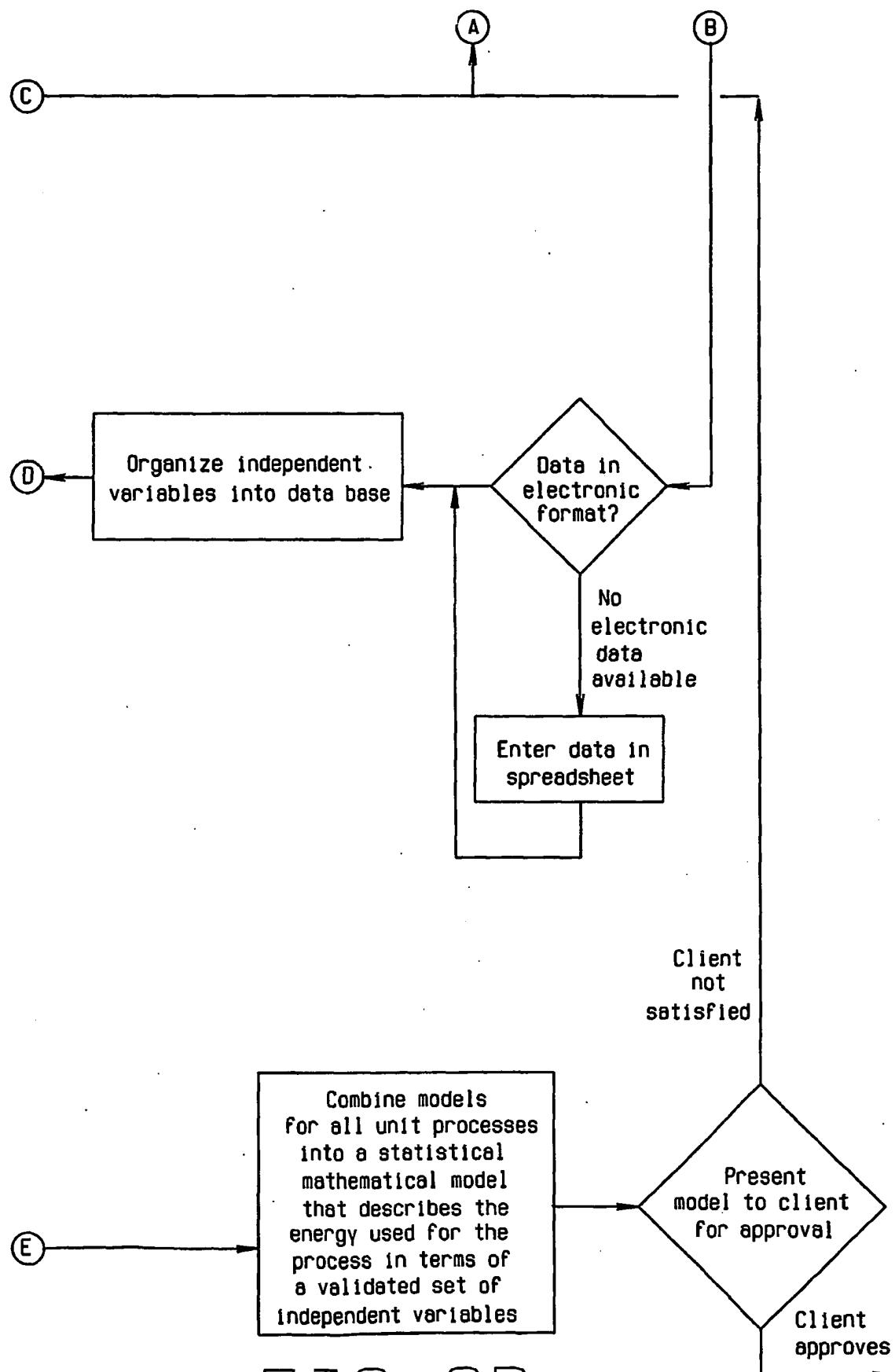


FIG. 2B

8/13

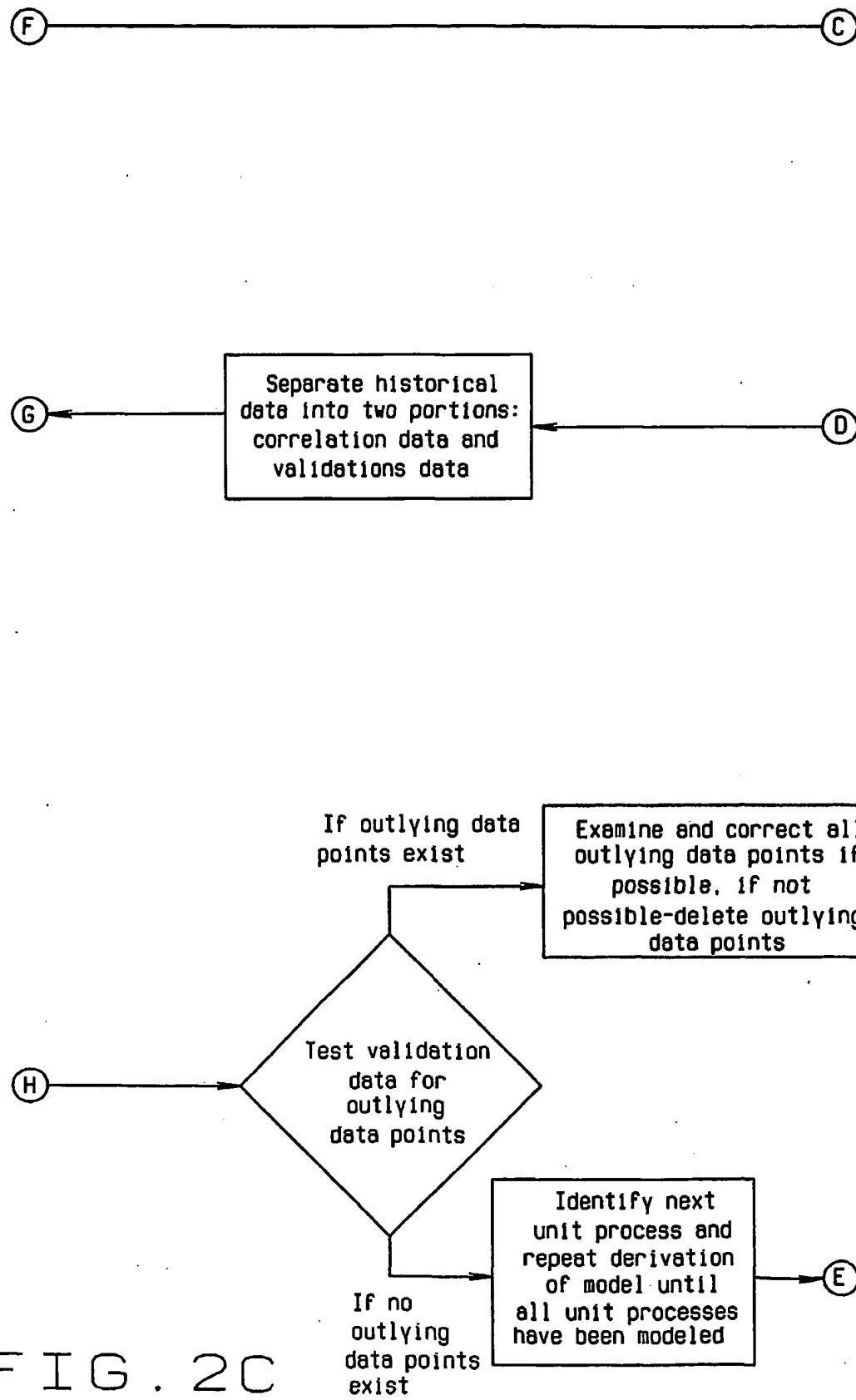


FIG. 2C

9/13

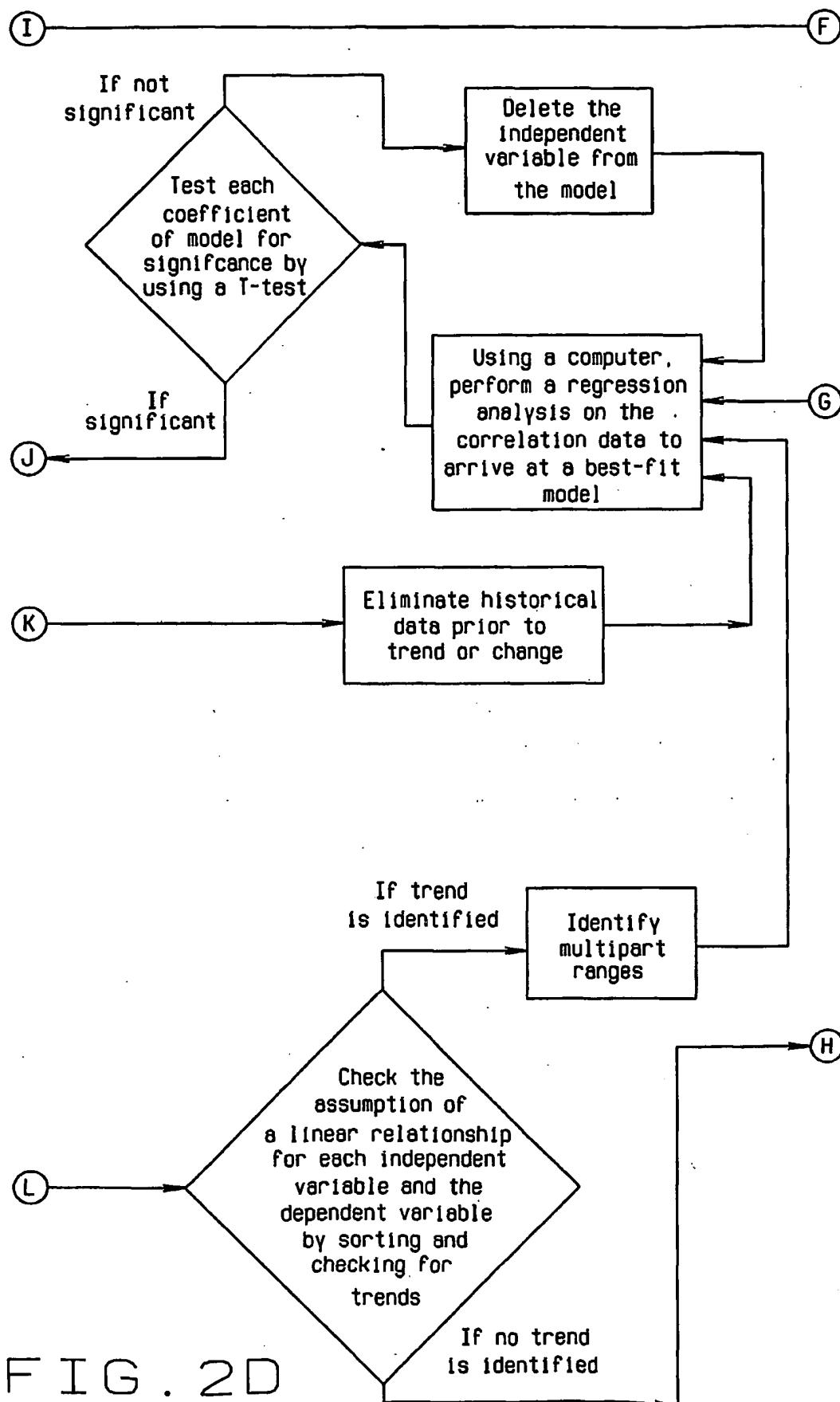


FIG. 2D

10/13

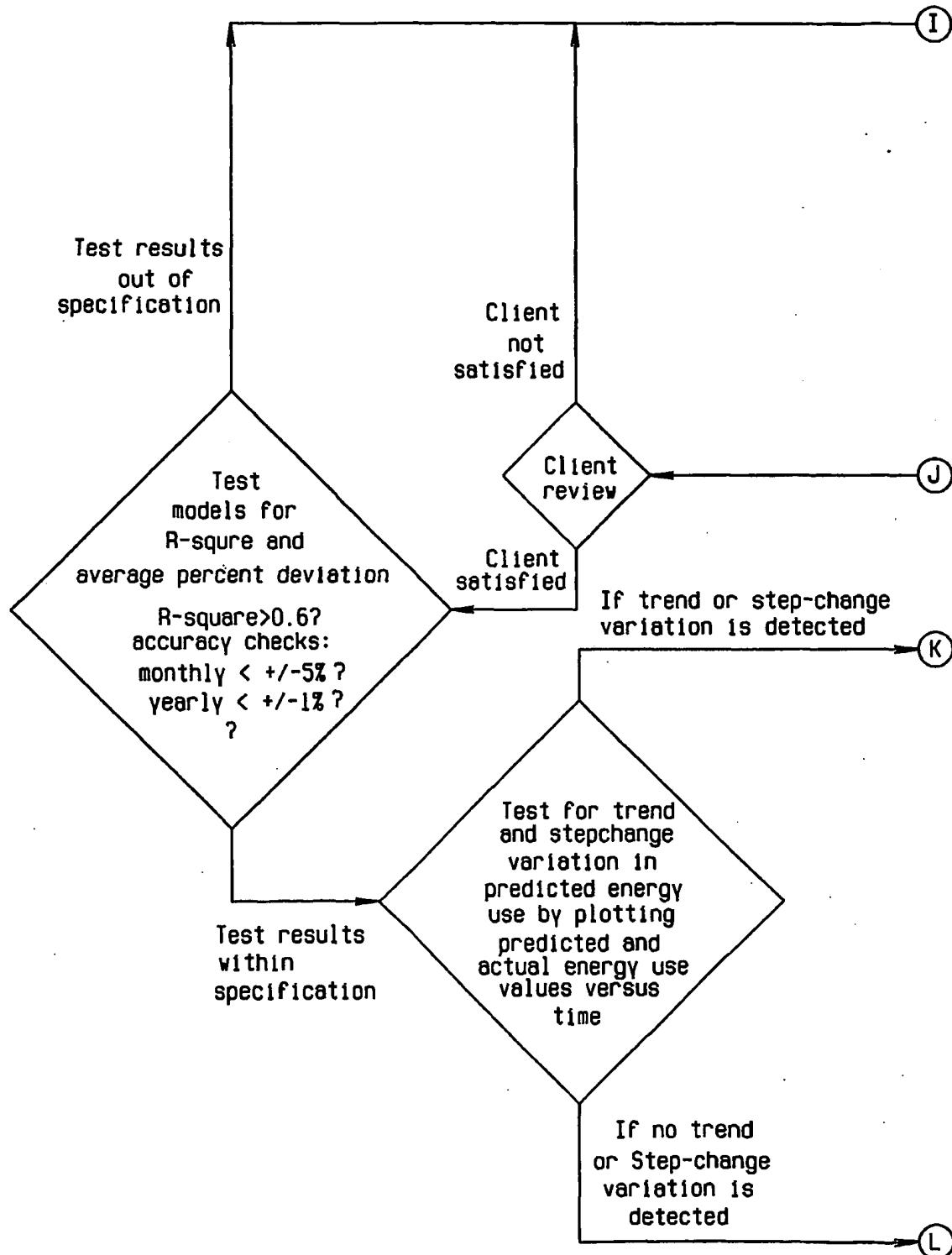


FIG. 2E

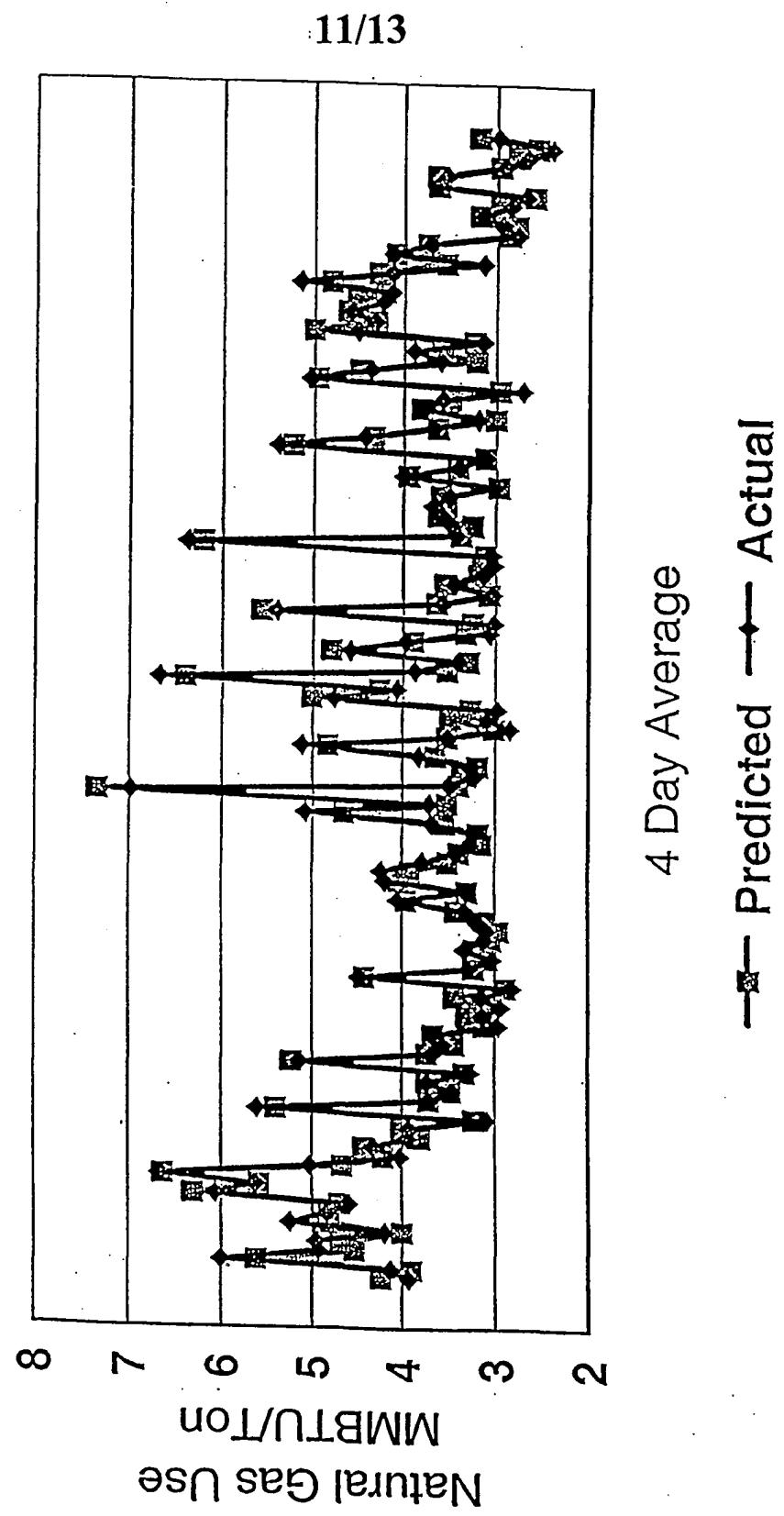


FIGURE 3.

12/13

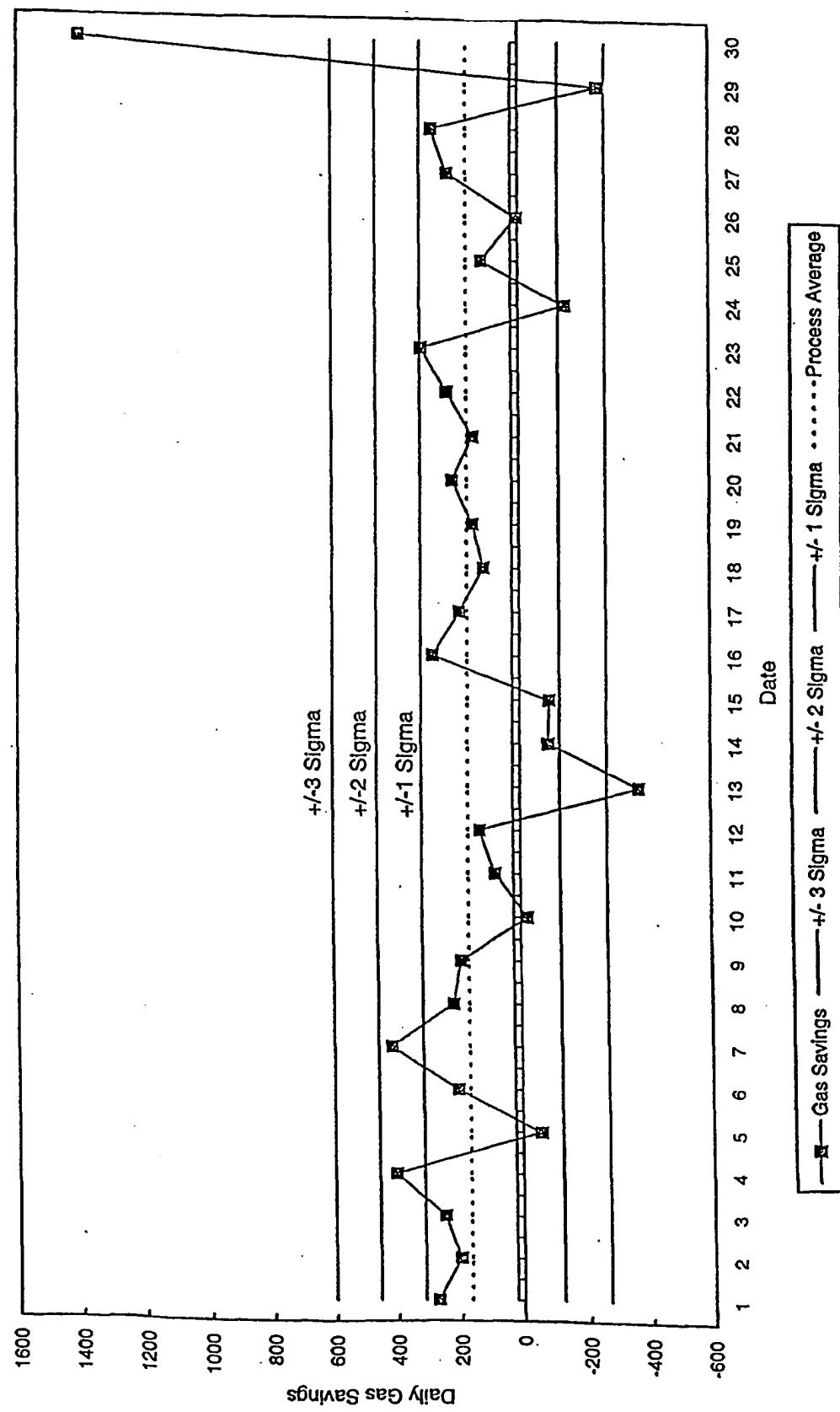


FIGURE 4.

13/13

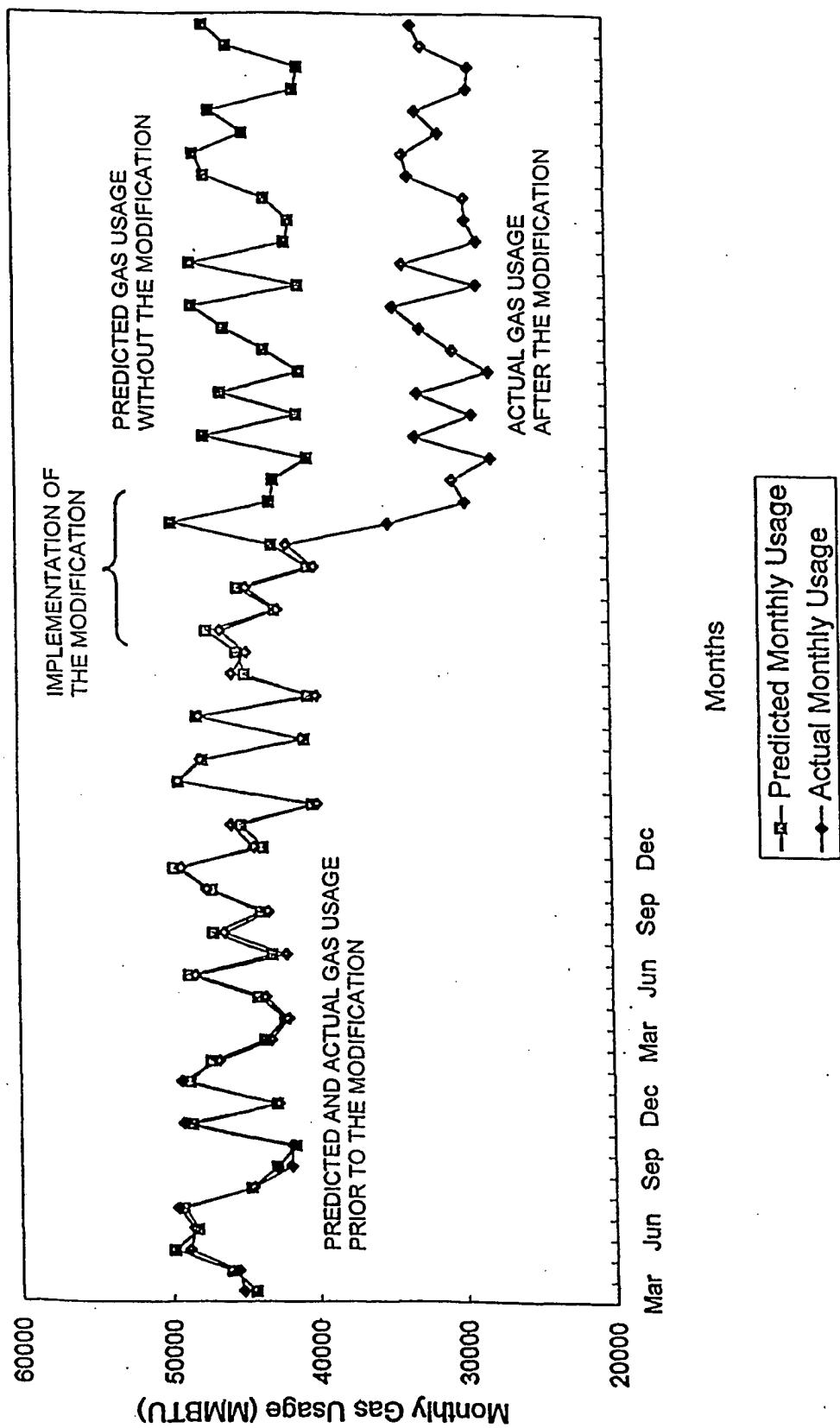


FIGURE 5.

## INTERNATIONAL SEARCH REPORT

International application No.  
PCT/US00/16270

## A. CLASSIFICATION OF SUBJECT MATTER

IPC(7) :G06F 7/60

US CL :703/1, 2, 3, 7, 11, 12; 705/7, 24, 34

According to International Patent Classification (IPC) or to both national classification and IPC

## B. FIELDS SEARCHED

Minimum documentation searched (classification system followed by classification symbols)

U.S. : 703/1, 2, 3, 7, 11, 12; 705/7, 24, 34

Documentation searched other than minimum documentation to the extent that such documents are included in the fields searched

Electronic data base consulted during the international search (name of data base and, where practicable, search terms used)

STN, PROQUEST, IEEE

search terms: energy, savings, contract\*, regression\*

## C. DOCUMENTS CONSIDERED TO BE RELEVANT

Category*	Citation of document, with indication, where appropriate, of the relevant passages	Relevant to claim No.
Y	COWAN et al. Measuring Energy Savings For Modernization Projects. ASHRAE Journal. August, 1997. pp. 60-63, especially p. 62.	1-4
Y	SONDEREGGER. A Baseline Model for Utility Bill Analysis Using Both Weather and Non-Weather-Related Variables. ASHRAE Transactions. 1998. pp. 859-870, especially pp. 861-862.	1-4
A	AUSTIN. Regression Analysis for Savings Verification. ASHRAE Journal. October, 1997. pp. 57-58.	1-38
A	ANONYMOUS. Keys to a Successful Performance Contract. American School & University. December, 1997. pp. 6-7.	1-38

 Further documents are listed in the continuation of Box C.  See patent family annex:

* Special categories of cited documents:	"T"	later document published after the international filing date or priority date and not in conflict with the application but cited to understand the principle or theory underlying the invention
"A" document defining the general state of the art which is not considered to be of particular relevance		
"B" earlier document published on or after the international filing date	"X"	document of particular relevance; the claimed invention cannot be considered novel or cannot be considered to involve an inventive step when the document is taken alone
"L" document which may throw doubts on priority claim(s) or which is cited to establish the publication date of another citation or other special reason (as specified)	"Y"	document of particular relevance; the claimed invention cannot be considered to involve an inventive step when the document is combined with one or more other such documents, such combination being obvious to a person skilled in the art
"O" document referring to an oral disclosure, use, exhibition or other means	"&"	document member of the same patent family
"P" document published prior to the international filing date but later than the priority date claimed		

Date of the actual completion of the international search

23 AUGUST 2000

Date of mailing of the international search report

20 SEP 2000

Name and mailing address of the ISA/US  
Commissioner of Patents and Trademarks  
Box PCT  
Washington, D.C. 20231

Facsimile No. (703) 305-3230

Authorized officer

KEVIN TESKA

*James R. Matthews*

Telephone No. (703) 305-9704

## INTERNATIONAL SEARCH REPORT

International application No. PCT/US00/16270
---

## C (Continuation). DOCUMENTS CONSIDERED TO BE RELEVANT

Category*	Citation of document, with indication, where appropriate, of the relevant passages	Relevant to claim No.
A	LEFEVRE. The Energy Efficiency Project Manual: The Customer's HAndbook to Energy Efficiency Retrofits: Upgrading Equipment While Reducing Energy Consumption and Facility Operations and Maintenance Costs. 1997.	1-38
A	SCHILLER et al. Measurement and Verification (M&V) Guidelines for Federal Energy Projects. Version 2.0. February, 1996.	1-38